COARSENINO OF CEMETITE PARTICLES IN Fe-0.74 C-0.37 Si ALLOY

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By A. SARANGI

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CERTIFICATE

This is to certify that this work on "Coarsening of Cementite Particles in Pe - 0.74%C - 0.37%3i Alloy" has been carried out by Mr. A. Sarangi, under my supervision and that this work has not been submitted electhere for a degree.

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ABSTRACT

Experiments were conducted to study the effect of 0.37% silieon on the coarsening kinetics of cementite in a 0.74%0 steel at 630°C. 660°C. 690°C and 710°C. Coarsening was found to be diffusion controlled. Particle size distribution did not reach a steady state. The coarsening rates of individual particles were calculated from particle eise distribution. The activation energy for the coarsening process was 51.03 Keal/gm-atom, Silicon also decreases the -Fe/Fe₂C interfacial energy. The activation energy during coarsening was found to be between those for earbon diffusion and iron diffusion in ferrite.

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CHAPTER 1

INTRODUCTION

A system of particles of a phase dispersed in a matrix has a tendency to reduce its total surface free energy. Because the surface to volume ratio of smaller particles is larger than that of larger particles, the average particle size increases with time. This phenomenon is called coarsening and is seen in many alloys of interest. Our understanding of the coarsening kinetics has been considerably enhanced by the theoretical and experimental investigations carried out in the last decade. However, much more work has to be done so that clear ideas about coarsening mechanisms may be developed.

A thorough understanding of the coarsening kinetics in steel has practical as well as theoretical importance. The loss of strength of steel during tempering is due to the coarsening of carbides. The sensitivity of mechanical properties to temperature and rate of spheroidisation are controlled by the coarsening mechanism. From the theoretical stand point, the understanding of coarsening mechanism in steels may help us to understand the coarsening behaviour in other systems. Also data on surface energy obtained from coarsening studies are useful in the study of numberation and growth.

In the work reported here, kinetics of coarconing of comentite in Ye = 0.74% G = 0.37% Si alloy have been investigated as a function of time and temperature.

LITERATURE REVIEW

2.1 Theory of Coarsening:

In a supersaturated solid solution diffusion effects can cause precipitation of a second phase. Three stages of this process can be distinguished. In the first stage, concentration and structural fluctuations produce nuclei of the new phase. In the second stage, growth of nuclei occurs directly from the super saturated medium and the concentration of the solute in the matrix decreases with time. In the third stage, larger particles grow at the expense of the smaller particles. This stage is called 'Coarsening' or 'Ostwald ripening'. The driving force for the process is the tendency of the system to decrease its over all free energy by reducing the total interfacial area,

Consider a precipitate of radius 'r' in the matrix. The pressure difference across the surface of the sphere can be written as

where, P_{pt} - Pressure inside the precipitate of relius 'r'.

P_{pt} - Pressure in the matrix.

Te Surface energy of precipitate.

The above equation is derived assuming that a single average value of 7 can be used for the various parts of the surface and that

the shape of the precipitate does not change when the size changes. If the precipitate consists of only one species and surface energy and density of precipitate are independent of its size, than at constant temperature we can write

where, r = Chemical potential of precipitate of size 'r'.

Vm = Molar volume of precipitate.

Assuming the compressibility of the solid to be small and using equation (1) and (2) it can be shown that

where, \int_{∞}^{μ} = Chemical potential of particle of infinite size.

It is seen from equation (3) that the chemical potential of small particle is larger than that of a large particle. Hence, it follows that concentration of solute in the matrix in equilibrium with smaller particle is larger than for a larger one.

Assuming the matrix to be dilute solution where the setivity of the solute is directly proportional to its concentration, the precipitates to be incoherent and the precipitate interface is free from preferential solute adsorption, the following equation called Gibb#s-Thomas equation can be derived

where, O, a Compositration of solute in the matrix in equilibrium with posticle of radius re

Commentration of solute in the matrix in equillibrium with particle of infinite size. R = Ges constant.

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T - Absolute temperature.

Thus in a system consisting of mixed particle sizes concentration gradient exist which leads to the growth of larger particles at the expense of smaller ones.

The steps involved in any coarsening process are as follows:

- (1) Dissolution of solute from smaller particles in the matrix i.e., transfer of atoms across the particle-matrix interface.
- (2) Diffusion of solute in the matrix from regions near smaller particles to regions near larger one.
- (3) Deposition of solute on the larger particles, i.e. transfer of solute atoms across the interface between the matrix and the larger particle.

interface is much faster than the rate of diffusion of solute in the matrix, the coarsening process is called diffusion controlled. When the rate of matrix diffusion is much faster than the transfer of solute across the interface, the process is called interface controlled coarsening. A third probability arises when most of the particles are situated near the grain boundaries of the matrix and diffusion occurs along the grain boundaries. In such a case the process is termed grain boundary diffusion controlled coarsening. At higher temperatures lattice diffusion is expected to be more important where as at lower temperatures grain boundary diffusion may become more prominent.

2.2 Theory of diffusion controlled coarsening:

Following assumptions are made to derive an expression for the growth rate of a particle².

- (1) Diffusion of solute in the matrix is controlling the rate
- (2) Concentration gradients are independent of time.
- (5) Volume fraction of precipitate is very small and the interpretible distance is large.
- (4) Volume fraction of particles remain constant.
- (5) Jocal equillibrium exist at the particle matrix interface.
- (6) Gibb's-Thomas equation is applicable.
- (7) Precipitates have spherical shape and the solute concentration around each particle is spherically symmetrical.
- (8) Precipitate consist of only one species.
- (9) Diffusion coefficient of solute is independent of concentration of solute.

In the steady state, the rate of change of volume of a precipitate equated to the flux of solute gives,

where, D - Diffusion coefficient of the solute

O' - Concentration of solute in the matrix at a distance
R from the precipitate.

At any given time integrating equation (5) from R=r to $R=\infty$ i.e. $C^*=C_r$ to $C^*=C_r$ we obtain

where, C. - Concentration of solute in the matrix at a large distance from the particle.

If 2 $\gamma v_m \ll r$ RT the Gibb s-Thomas equation can be written as

$$O_x = O_e \left[1 + \frac{2V_{tt}\gamma}{x\Omega T}\right] \qquad (7)$$

Since the volume fraction of the precipitate is constant, in a system of n highly dispersed particles

$$\sum_{i=1}^{n} \frac{dV_i}{di} = 0 \qquad \dots \qquad (8)$$

Using equation (6), (7) and (8) and substituting \overline{r} , the arithmetic average radius for $\sum_{i=1}^{n} r_i/n$ we get

$$\frac{dF}{dt} = \frac{2C_0 \times V_B D}{2MT} \left(\frac{1}{F} - \frac{1}{F}\right) \qquad (9)$$

Theoretically, coarsening does not occur in a system of particles of the seme size. But in practice small thermal or other fluctuations will give rise to concentration gradients and will effect coarsening of some particles. Thus with increasing time, this limited size distribution of particles will become wider. However, the spread will be limited. It can be shown that the growth rate is maximum at r = 2r. The particles of radius greater than 2r will grow at a rate smaller than the rate of growth of smaller particles. It follows that particle of radius much greater than 2r can mot exist in the system. It implies that a relatively sharp cut off in the particle size distribution should exist. It may be noted that particles of size resister than F, grow at the expense of particles of size greater than F, grow at the expense of particles of size less than F, a sobsmatic plot of this is shown in figs. 1.

An expression for F can be derived by putting r = 27 in

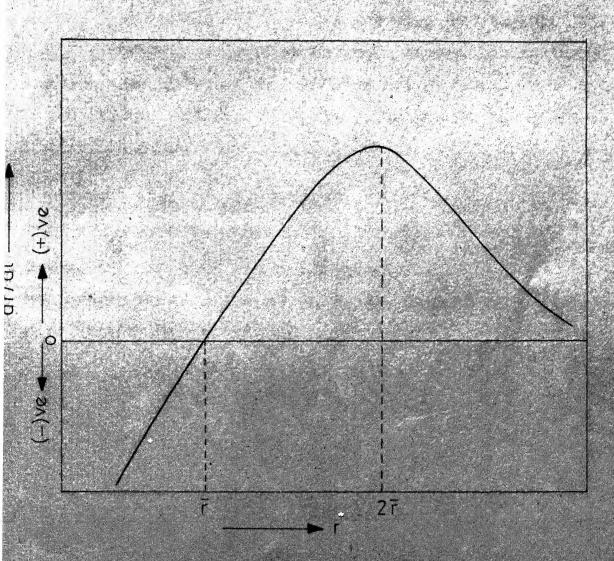


Fig. 1 Schematic plot of dr/dt vs.r for diffusion controlled coarsening.

equation (9) and integrating. We get

$$\vec{P} - \vec{P}_0 = (\frac{3 \cancel{0}_0 \cancel{V}_B D}{RT}) t \qquad \dots \qquad (10)$$

where, r = Average radius when coarsening just begins.

A rigorous analysis of diffusion controlled coarsening has been done by Wagner³ and Liftshiz and Slyozov⁴. This is known as WLS theory. Let f(r, t) be the particle size distribution function such that

$$\mathbf{H} = \int_{0}^{\infty} \mathbf{f}(\mathbf{r}, t) d\mathbf{r} \qquad \dots \qquad (11)$$

where, N = Number of grains per unit volume.

The unknown function f(r, t) can be determined from the equation of continuity in r space.

$$\frac{\partial x}{\partial x} + \frac{\partial (x, \frac{\partial x}{\partial x})}{\partial x} = 0$$
 (12)

and the equation for the conservation of matter is

$$Q_0 = Q_0 + \int_0^{\infty} \frac{1}{2} x^3 x(x, t) dx$$
 (13)

where, Q = Total amount of solute in the alloy in cm3/cm3.

C. - Average concentration of matrix at any instant t.

Using equation (6), (7) and (13) Vagner and Liftshiz and Slyosov solved the differential equation and showed that the particle cise distribution reaches a postuostatic form. The theory errives at the following results, where $P = \pi/2$

molar volume of cementite with the formula PegC and Ce is the concentration of earbon in the matrix in equillibrium with precipitate of infinite size.

Moreon has shown that cumulative size distribution function can be approximated by the following expression

$$C(P) = AP^4 \qquad (17)$$

whare

$$G(P) = \int_{P} P^{2} h_{1}(P) dP$$

and A = Constant.

Markworth⁶ has shown the following expression for the variation of size of individual particles with time

$$(\frac{3-2P_0}{3-2P})^{5/3} (\frac{3+P_0}{3+P})^{4/3} \exp \frac{6(P_0-P)}{(3-2P_0)} = \frac{1}{6} \cdots (18)$$

where,

to = The time when coersening just begins.

Exnel and Lukes tried to verify WLS distribution of the particle.

Ardell etudied the cumulative particle size distribution.

In the VLS theory it is assumed that the volume fraction of precipitate is very small and the motion of interface is not obstructed by the solvent atoms, i.e. matrix atoms move much faster than solute atoms. This is valid only in liquid fluid matrix. Hence diffusion coefficient in equation (15) is not merely diffusion coefficient of solute but some effective diffusion coefficient.

Ic, Blakely and Feingeld have developed a coupled diffusion analysis which considers composition constraint as well as volume constraint. In a coarsening process when the particle consist of more than one component, exchange of matter between the particles will in general be subjected to a composition constraint, requiring that the diffusive fluxes of the components of the dispersed phase be coupled in order to prevent change of composition of any particle. This composition constraint has the form

$$\frac{J_A}{J_B} = \frac{B}{5} \qquad \qquad \dots \qquad (19)$$

where the precipitate has the formula A B and the matrix consist of metal A.

The volume constraint arises from the fact that it is required to remove a volume of matrix material around a growing particle equal to the volume by which that particle has grown in order to avoid any elastic strain energy in the system. This may be expressed as

$$J_1V_1 + J_2V_2 = 0$$
 (20)

where J_1 and J_2 are flux of solute and solvent respectively. V_1 is the volume made available by the transfer of one gm. atom of solute from the particle to the matrix and V_2 is the atomic volume of solvent in the matrix Lt et al⁹ have derived effective diffusion coefficient for such cases. The expression is given below

$$D_{\text{eff}} = \frac{c_0 D_1 D_2 V_2 (V_2 + c_1/c_2 \times V_1)}{c_0 D_2 V_2^2 + c_1 D_1 V_1^2} \cdots (21)$$

For the iron-carbon system this can be written as

$$\mathbf{B_{eff}} = \frac{\mathbf{C_{Fe}} \ \mathbf{D_{Pe}} \ \mathbf{V_{Pe}^{2}} + \mathbf{C_{G}} \ \mathbf{D_{C}} \ \mathbf{V_{Pe}^{2}}}{\mathbf{C_{Pe}} \ \mathbf{D_{Pe}} \ \mathbf{V_{Pe}^{2}} + \mathbf{C_{G}} \ \mathbf{D_{C}} \ \mathbf{V_{C}^{2}}} \ (\mathbf{V_{Fe}} + \frac{\mathbf{C_{G}}}{\mathbf{C_{Pe}}} \ \mathbf{V_{C}}) \ . \ . \ . \ (22)$$

where subscript Fe and C stand for iron and carbon respectively. Since $D_{p_0} \ll D_C$ and $\frac{G_C}{G_{p_0}} \, V_C \ll \, V_{p_0}$ equation (22) can be written as

$$D_{eff} = \frac{c_{p_0} v_{p_0}^2}{c_0 v_0^2} D_{p_0}$$
 * * * * * (23)

Determination of D and y :

Rastogi and Ardell¹⁰ and Ardell^{11,12} have emphasized the importance of concurrent measurement of \vec{r} and C during coarsening. If such measurements are made γ and D can be known independently. Otherwise to evaluate D we must know the value of γ and vice versa. Since the rate constant after equation (15) is

where K is the experimental rate constant for the growth of particles. Ardell^{11,12} and Rastogi and Ardell¹⁰ have shown that for matrix composition

where

From equation (24) and (26) we get,

$$n_{\text{eff}} = \frac{9}{4} \frac{(\kappa^2 \kappa^2)^{1/3}}{\pi}$$
 ... (27)

and

$$\gamma = \frac{(\mathbb{K}/\mathbb{K}^1)^{1/3}}{2} \qquad \dots \qquad (28)$$

With the help of equations (27) and (28) values of $D_{\rm eff}$ and γ can be obtained. Though it is assumed that in Ostwald ripening the amount of solute in the matrix remains constant, the equation (24) and (26) can still be taken advantage of with reasonable assumption that interface energy γ does not change with composition of the matrix appreciably and also is independent of particle size. This assumption breaks down if the particles are so small that they are coherent with the matrix.

Effect of Volume Praction on Coersening Rate:

The theory of diffusion controlled coarcening developed by VIS assume that the volume fraction of precipitate is so small that it does not effect the diffusion passage of solute atoms. Ardell¹⁵ in a recent paper has theoretically considered the effect of volume fraction on particle coarcening. His expression for average radius is given below

whore

that the second

 $V(\beta) = A$ function of volume fraction β

$$(\beta) = \frac{3P_{m}^{2}}{\beta P_{m} + (1 - \beta)P_{m} - 1} = \frac{3P_{m}^{2}}{1 + 2\beta P_{m} - \beta}$$

$$\beta = \frac{66\sqrt{3}}{\sqrt{3}}$$
(30)

where

 $\Gamma(\beta)$ is enother function of β

$$P_{m} = \frac{(\beta^{2} + \beta + 1)^{\sqrt{2}} - (1 - \beta)}{\beta} \qquad (51)$$

The new parameter P_m is the theoretical relative maximum particle size of the polydispersed assembly. The theoretical distribution of particle size must go to zero when $P \gg P_m$. When $\beta \to 0$, $\mathcal{D}(\beta) \to \frac{27}{4}$ and $P_m \to \frac{1}{2}$ and as $\beta \to \infty$ $(\beta-1)$ $\mathcal{D}(\beta) \to 0$ and $P_m \to 2$. This analysis shows that the coarsening rate should increase without limit as the volume fraction increases towards unity. Furthermore, the maximum particle size approaches twice the critical size, so that we can expect a broadening of the theoretical particle size distribution as β increases. The complete dependence of \mathcal{D} , P_m and β has been reported.

2.3 Theory of Interface Controlled Coarsenings

According to Greenwood²⁰ the rate of interface controlled operating of an individual particle is given by

where B is a constant. Using equation (7), (8) and (32) we can write

$$\frac{dr}{dt} = \frac{2\sqrt{c_0 V_B B}}{RT} (\frac{1}{T^*} - \frac{1}{T})$$
 ... (35)

where

$$r^* = \text{Critical radius} = \frac{\int_0^\infty r^2 f(r, t) dr}{\int_0^\infty r f(r, t) dr}$$

Wagner has analysed this case in detail using equation (7), (13) and (32), and solved equation (12). His results are

$$f(P, T) = H(t) Ph_2(P)$$
 $Ph_2(P) = P(\frac{2}{2-P})^5 exp(-\frac{3P}{2-P}) \text{ for } P \leq 2$
 $Ph_2(P) = 0 \text{ for } P > 2$ (34)

where $P = \frac{F}{F^*}$

Wegner also showed that

and

Kirchner¹⁴ has shown that the cumulative size distribution of particles due to interface controlled coarsening is given by

Markworth bas shown that the variation of individual particle is given by

$$\left(\frac{2-P_0}{2-P}\right)^2 \exp \frac{x(P_0-P)}{(2-P)(2-P_0)} = \frac{1}{k_0} \cdots (57)$$

where again $P = \frac{F}{F^*}$ and $P_0 = (\frac{F}{F^*})_{\xi_0}$. The above equation is applicable only for $t < \xi_0$.

2.4 Theory of Grain Boundary Diffusion Controlled Coarsening:

If all the precipitates are situated near the grain boundaries of the matrix and if it is assumed that the diffusion of solutes occurs only along grain boundaries (not a very good assumption at high temperatures) the kinetics of coarsening is altered. Speight 5 writes the following modified Gibbs-Thomas equation for this case as.

$$C_{x} = C_{0.50} \exp(\frac{2\sqrt{v_{20}}}{x^{1/2}})$$
 (38)

where.

- Cp Concentration of solute on the grain boundary in equilibrium with particles of radius r.
- Co.g. = Concentration of solute on the grain boundary which is in equilibrium with particles of infinite size.

Using a method similar to that of Greenwood, Speight is bee derived an expression for the rate of convening of grain boundary particles which is given below

abore

Dg = Grain boundary diffusion coefficient

w - Width of the grain boundary

$$=\frac{2}{3}-\frac{7}{27}+\frac{1}{3}(\frac{7}{27}-\frac{1}{3})^3$$

 y_{g,b_*} = Surface free energy per unit area of the boundary h = $\frac{1}{5} \ln (\frac{1}{4})$

f = Practional area of grain boundary occupied by the particles.

The variation of average particle size with time is given by

$$\vec{x}^4 - \vec{x}_0^4 = \frac{4 / V_m C_{0+g_0} D_g V}{3 8 B M} + \cdots$$
 (40)

Kirchner¹⁶ has applied WIS type of analysis to the coarsening of grain boundary precipitate. He found that the distribution function reaches a quasi stationary state after long periods of time.

Rirchmer 14 has also shown that cumulative distribution function for pseudostatic distribution of grain boundary particle convening can be approximated as

In a recent paper Ardell[©] has derived cumulative distribution function for the grain boundary precipitate. The effect of volume fraction is also included in the derivation.

Markworth and Glamer's following VIS type of analysis have also derived an expression for the sayaptotic size distribution function.

Ardell¹⁷ has studied the behaviour of grain boundary precipitate in a medified way. His results also confirm the r⁴ law for the growth of grain boundary precipitate, when grain boundary diffusion is rate controlling factor.

2.5 Effect of Alleying Element on Coarsening Mechanisms

The above theories are applicable to binary alloy only. The effect of a third element on Ostwald ripening has been considered in detail in a quantitative manner by Bjorkuland et al 19. The termsky rate equation derived for Fe-C-X matrix is

$$\frac{dx}{dt} = \frac{2 \gamma V_{m} D^{t}}{3RT(1-K_{s})^{2} v_{T}^{2}} \frac{1}{r} (\frac{1}{r_{0}} - \frac{1}{r}) \qquad * * * * * (43)$$

and the rate of coarsening after long time is given by

$$x_{0}^{3} = \frac{8 \gamma V_{0} D^{4}}{27RT(1 - K_{0})^{2} U_{0}^{6}} * \cdots (44)$$

Theratio of the rate constant for the binary and ternary cases will be

$$\frac{X_{\text{borneyy}}}{X_{\text{binary}}} = \frac{D^{4}}{3(1-X_{4})^{2}} \frac{D^{6}}{D_{0}} \frac{U_{0}^{6}}{U_{2}^{6}} \cdots (45)$$

whore

D' . Diffusion coefficient of element I.

The second of observed I be converted to an extension?

Be a property of element X in separate in an moles/as

UX = Alloy content at the surface of particle of oritical radius r.

U = Ordinary solubility of comentite in ferrite.

The U parameters are given as

where x stands for mole fraction and the subscripts X. Pe. o for alloying element, iron and earbon respectively.

2.6 Coarsening in Non-Perrous Alloys:

Many investigators have studied coarsening in non-ferrous alloys. The results of these investigations are listed in table to

2.7 Coersening in Ferrous Alloys:

Day and Baiford studied commoning of comentite in Pe-O.3%C alloy at 675°C and 720°C. Average particle size was measured by using Pullman's method for monodispersed system (i.e. all particles have some size). At 720°C the slope of log F vs log t was nearly sero at small tempering times and at longer time it approached a value of 0.33. At 675°C they found a break in the log F ve log t plot. At small tempering time the

slope was nearer to 0.33 while at longer tempering time the slope was found to be nearer to 0.25. It was concluded that at 720°C comentite coarsens by a diffusion controlled process, but at 675°C for longer tempering times the grain boundary diffusion appeared to be a rate controlling factor. However Pullman's enalysis can be not be applied for a coarsening system since we have a range of particle size.

Heckel and Degregorio⁴⁴ studied convening of comentite in Pe-O.75%C alloy at 704°C. Particle size distributions were measured by using Dehoff's method. The size distribution were found to be log-normal. Data were analysed by using Heckel's⁴⁰ model, which is similar to WIS model but requires no specification about shape of the particle size distribution curve. However, Heckel's⁴⁰ model assumes that number of particles, per unit volume, of different sizes is same. Coarsening of cementite in this steel appeared to obey an interface controlled kinetics.

Vedula and Heckel³⁹ investigated coarsening of comentite in binary Fe-C alloys, 0,24, 0,42 and 0,79 wt/C at three temperatures 594°C, 649°C and 704°C for times up to 10^6 secs. It was found that particle size distribution did not reach a steady state even after tempering for 10^6 secs. Analysis of data using Heckel's 40 model indicated that coarsening of comentite in these steels is a diffusion controlled process. Flots of $(\frac{10^3}{2} - \frac{10^3}{2})$ to a were linear and approached a slope of 1_2 O at high temperatures only. Deviations of slope at low temperatures were attributed to noneteely state distribution.

Gokhale 46 and Verma 47 have also studied the coarsening of cementite in Pe-0.79%C alloy. They found the coarsening mechanism to be diffusion controlled. Mehl et al42 studied coarsening of comentite in Fe-O. 15%C. Fe-O. 15%C - 1980. Fe-C. 15%0 - 1%Ni and Fe-C. 15%C - 1%Or alloys. A series of tempering temperatures between 500°C and 700°C and tempering times of up to 190 hr. were used. Out of these Fe-C-Cr system could not be studied due to precipitation of double carbides. Plots of F ve t were linear in all other cases but there was some scatter at lower tempering temperatures. Size distributions were much more broader than predicted by VIS theory. It was also found that cold working of earples before tempering did not have any effect on the rate of coarsening. It was observed that nickel did not have much effect on the coarsening rate. but manganese decreases the rate markedly. The value of surface energy of cementite-ferrite interface is expected to lie in the renge of 500 to 1000 ergo/on . Exceptionally high values were obtained at lower tempering temperatures. It was suggested that rate of communing in these steels is determined primarily by volume diffusion at high temperatures, but the grain boundary diffusion plays en increasingly important role as the tempering temperature is lowered.

Cokhale to has studied coursening of comoutive in FewO.79%C + O.45%Si alley at 690°C. He found the coursening mechanism to be diffusion controlled. It was also observed that Si decrease the rate of coursening.

Muchanjes et al 49 investigated kinetics of coarsening of carbides in a ceries of Pe-0,20%C - Cr alleys at 700°C. It

was found that the coarsening rates of the carbides decrease in the order Fe₃C : K₃C : K₂C₅ : K₇C₃. The kinetics of coarsening in recrystallised steels indicate that the process is diffusion controlled. K₅C and K₇C₅ are shown to coarsen at rates expected if diffusion of chromium is rate controlling, but Fe₅C coarsens too rapidly for the equivalent diffusion of iron to be controlling. In as tempered steels, the dislocation structure of the matrix inherited from martensite leads to coarsening rates greater than the predicted value.

Bannyh³⁶ et al as quoted by Greenwood³⁷ were the first investigators to obtain quantitative experimental data in steels. They studied commenting in a commercial 0,83%C steel. The tempering temperature ranged from 210°C to 710°C and time from 1.5 sees to 20 hrs. The plot of F⁵ vs t was found to be linear at 700°C. At lower temperatures agreement with WIS theory was poor. They concluded that the coersening was diffusion controlled. They did not study particle size distribution.

Dirnfeld⁴⁸ studied the coarsening kinetics of comentite in outcotoid steel, of commercial purity with 0,89% and 0,28% Al. Their investigation shows that the reaction was diffusion controlled.

Cokhale 46 also studied the coarsening of cementite in eutertoid steel of commercial purity. He found that the coarsening was diffusion controlled.

Holfs of al bure studied dissolution kinetics of commutate in ferrite by resistivity measurements and data were

correlated to average carbon concentration in the matrix. It was concluded that dissolution of cementite in ferrite is entirely an interface controlled process.

Harris et al⁴⁴ studied the growth kinetics of graphite in Fe-C-Si system. According to them the graphitization obeys an equation of the form

$$y = 1 - \exp(-\frac{t}{R})^{2}$$

n taking values close to 3.0; y is any parameter for growth rate in graphitization. They also concluded that in most part of reaction diffusion of C in ferrite is rate controlling factor.

2.8 Quantitative Metallography:

Quantitative metallography methods are required to measure the particle size distribution in metallurgical processes such as recrystallization and mucleation, growth of precipitate particles etc. Several analysis have been made for determining spatial size distributions from two dimensional measurements. In general, the analysis are based on the assumption that (a) the particles have spherical shapes, (b) the distribution of particle sizes is broken up in to descrete size groups.

These methods may be classified in to three major categories according to type of planar measurement performed. These extegories are based on:

- (a) Distribution of section disputer
- (b) Distribution of section areas
- (a) Distribution of section short lengths

All the methods are based on the statistical probability of the plane intersecting a sphere of diameter D_j so as to produce a section of size d_j . The probability may be expressed in terms of radii as

$$P_{i,j} = \frac{1}{k_j} \left(e_i R_j^2 - x_{i-1}^2 - \sqrt{R_j^2 - x_i^2} \right) \dots (47)$$

Let us now consider a polydispersed system of spheres that has been separated in to five class intervals. The number of spheres per unit volume in each class interval is represented by N_j , j=1,5 and corresponding radii are R_j , j=1,5.

The total number of circular sections of given size per unit armis n_1 , n_2 , n_3 , n_4 , n_5 where the section radii vary from 0 to R_1 , R_1 to R_2 , R_2 to R_3 , R_5 to R_4 , R_4 to R_5 respectively.

Spheres of the largest class interval yield sections of all radii when out by a random plane. Therefore, the observed number of sections of the smallest size per unit area, n_i , is the sum of contributions from spheres of all sizes. So we can write

$$m_1 = \sum_{j} m_{1,j} = m_{1,1} + m_{1,2} + m_{1,3} + m_{1,4} + m_{1,5}$$
 **(48)

We want to calculate the number of spheres per unit volume in each class interval. In order to do so the number of sections having the same radius as their spheres $(X_{1,1})_1$ $(X_{1,2})_2$ etc. are determined. In this sace equation (40) becomes

$$H_{3,3} = h_3 - H_{3,5} - H_{3,4}$$
 $H_{2,2} = h_2 - H_{2,5} - H_{2,4} - H_{2,3}$
 $H_{1,1} = h_1 - H_{1,5} - H_{1,4} - H_{1,5} - H_{1,2}$

(49)

Since n_5 is measured quantity $N_{5,5}$ is known, $P_{5,5}$ is calculated from equation (47), and D_5 is measured from the plane of polish. We can now calculate N_5 from the equation

$$u_{3} = \frac{\sum_{1}^{N} u_{1,3}}{2} \frac{1}{2}$$
(50)

Knowing N_5 we proceed to calculate N_4 . This sequence of calculation is continued down to the smalles particles size.

Let us now discuss a few important methods for transforming two dimensional measurements in to corresponding three dimensional distribution.

Schwarts-Saltykov⁵⁰ (diameter) analysis:

The particle size may be broken down in to any number of groups up to 15, depending up on the accuracy required. The number of groups should not be less than 7. If the largest diameter is D_{max}, and K be the total number of groups them,

Place the dismeter of the particles of the first groups is \triangle , that of the second group is $2\triangle$ etc. To properly identify the number of sections of a particular class interval both section size and particle size must be specified. Index j indicates the group of particles which form the given sections

on the plane of polish. Index i refers to the size groups of the sections. Thus for example, N_{3,4} indicates the number of sections of the third size group (with diameter between 2 and 3) formed exclusively from 4th size group (with dia equal to 4). With this notation we can write total number of sections of the first size group as

$$m_1 = \sum_{j=1}^{K} M_{j,j} = M_{1,1} + M_{1,2} + M_{1,3} + \cdots + M_{1,2} + \cdots + M_{1,K}$$

Similarly for the second size group

$$n_2 = \sum_{j=2}^{K} n_{2,j} = n_{2,2} + n_{2,3} + n_{2,4} + \cdots + n_{2,1} \cdots + n_{2,K}$$

and so on.

The total number of particles per unit volume is

The probabilities that a random plane will intersect spheres of the various diameters to give particular sections are calculated as describe before. Equations are then set up for H, in terms of H, ... The latter terms can be eliminated by substituting n, values for H, ... Talues by the calculations as described earlier, leaving H, expressed as function of n, values i.e. the measured quantity. The general equation is

$$P_{3} \cdot \pm \sum_{i=1}^{\infty} P_{3,i} \cdot \cdots \cdot (51)$$

Though I can be calculated by summing H., it can be calculated

$$\Delta \qquad \sum \beta_{i,j}$$

Saltykov⁵¹ (Area) analysis:

This method does not require sequential calculations nor tables of coefficients. Saltykov adopt $A/A_{\rm max}$ to specify size of a section instead of the absolute area. The scale factor used to get class intervals for $A/A_{\rm max}$ is based on a logarithmic scale of dismeters with the factor $10^{-0.1}$. The advantage of using $A/A_{\rm max}$ to group the sections lies in the unique relationship of particles shape to the n versus $A/A_{\rm max}$ frequency distribution.

The computations follow along lines described previously. The results of the successive calculations give a general working formula which gives N_j directly for any desired class interval.

$$H_{3} = \frac{1}{D_{3}} = 0.6461 \, m_{3} = 0.4561 \, m_{3-1} = 0.1162 \, m_{3-2} = 0.0415 \, m_{3-3} = 0.0079 \, m_{3-5} = 0.0038 \, m_{3-6} = 0.0018 \, m_{3-7} = 0.0018 \, m_{3-6} = 0.0008 \, m$$

Evidently not more than 12 class intervals should be used. The method is direct and simple. It is applicable not only to polydispersed systems of apherical particles but in principle convex particle as well.

The Spakkov⁵² (Chart) evaluates

In this analysis a random line is passed through a section plane and shord lengths of the particles out by the test

line are measured. They are grouped in to number of size classes. The size interval is fixed as in diameter analysis.

The working equation is

$$N_{3} = \frac{4}{77\sqrt{2}} \frac{(n_{1})_{4}}{23-1} - \frac{(n_{2})_{3+1}}{23+1} \cdots (53)$$

where, H_j and $(n_L)_j$ are the number of particles per unit volume and the number of chords per unit length of test line, respectively for the indicated jth size class. The equation is very handy and simple in its use.

Spatial size distribution of non-spherical particles:

It is obvious that computational complexities increase considerably in the analysis of size distribution of non-spherical particles. Wicksell⁵³ was first to give an analysis for ellipsoidal particles. Wicksell's analysis is very lengthy and mathematically complex.

Recently analysis for ellipsoids have been published by Dehoff's analysis for oblate ellipsoids was used in our investigations and given in detail in chapter 4.

Peulus⁵⁵ has analysed a little more difficult care of pentagon and dedicabedron while Cahn and Pullman⁵⁶ have analysed the lamellar structure.

2.9 Scope of Present Investigations

It is clear from above that the results of previous workers on convening of comentite in steels are conflicting. Day and Balford found that commenting of comentite is grain

boundary diffusion controlled. The investigation of Heckel and Degregorio⁴¹ shows that it is interface controlled process. Vedula and Heckel⁵⁹ showed it to be volume diffusion controlled process. Moreover the effect of alloying elements have not been investigated extensively. Particularly of silicon not been investigated except the work of Gekhale⁴⁶. He has done some preliminary work on the effect of silicon in a 0.73%C steel. He carried out his investigations at 690°C only. As no thorough investigation has yet been carried out on the effect of Si in the steel, it was decided to investigate the effect of silicon on the coarsening kinetics of cementite in steel as a function of temperature.

1	Teolonique used to messure ?	Torrienton of r with time with	Particle stre distribution	Conclusion	Romerte	Boferen
				Diffusion controlls growth	Despite the fact that lattice mismatch between Co and Cu is very large and strain field results from coherency, the variation of F with time seems to be unaffected.	53
3.1			Metribution reaches a questiones y state but out off tends to be more than 1.5.	Diffueton controlled growth	Agreement of F vs t 22, with Wis theory even when particles are very close together shows dominating effect of concentration gradient mear the particle surface.	22, 23
				Southeaten Southeaten	For particles in the 24 news and to be resonable correlation between and deviation of experimental deviation of experimental that predicted by the crystics of the larger is the deviation.	29 ਨ ਰ :

8	8	F a second	% %	8	
fresh te		times 27 relat- setivation growth s that of of solute s particle a energy f reases and more nearly	25 and 45	848 B	
only when the different is a significant in the significant in the significant is a significant in the significant is a significant in the		th rate is relat- f high and setivation f for the growth approaches that of wion rate of solute At large particle activation energy growth increases and	a of	to Cu reduces of the Current of the	
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Diffusion theory i obeyed only when wariable diffusion coefficient is app D = D _o (1 + K _p)		Though at low times 27 growth rate is relat- ively high and setivation energy for the growth rate approaches that of diffusion rate of solute atoms. At large particle ston growth increases and appears to be more nearly	dependent solely on the	A trace addition to to Cu reduces sening rete of Or probably reduction interfacial energ	
Mffusion controlled coarsening	Diffusion controlled coarsening	Decomposition of SiO, in matrixita rate control-		Diffusion controlled growth for er and short circuit di-	
- \$ 6	16				
	- 9				
Metributions were much prosder than the theore- tionl one	Distribution were in best agreement with theory.			•	
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The equilibrium shape 29 of the particles is that of rods with hemispherical caps and is due to large amisotropy in the copper/ -7e interfacial free energy (// = 4). The mean calculated radius was found to be smaller than those observed by a factor of ebout one helf.	It was found that shape 51, of the particle changes with time so WIS theory could not be applied	The growth rate of 35 largest particles were measured. It did not egree with WLS equation of growth rate since their expression is for growth average particle size	to obtained its process
Diffueton controlled controlled	Nonn free path was needed free free free free free free free	Diffusion controlled	It is not possible to decide from the data obtained whather the coarsening process is diffusion or interface
		Not studied	Sood agreement with both diffusion and interface controlled models
Maria de la companya			
			E III

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	86	* *	75
e de la companya de		in The value of n = 4 3 end 5 suggest that grain boundary diffusion and pipe diffusion play important roles.	The behaviour of commenting process at larger times has been attributed to the reduction of the diffusivity of the slowest moving atom species in the matrix
		Coerrenting to difficulties on the second controlled. Second con the second control con the second control con the second control	Addition of magnesium and inditially increases the coarsen- the coarsen- the coarsen- the coarsen- the rete of Allo, st. 1300% at 1300% at 1500% at
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CHAPTER 3

EXPERIMENTAL WORK

Coarsening of cementite in ferrite matrix was studied in Fe-C-Si alloy at four different temperatures. The temperatures selected were 710°C, 690°C, 660°C and 630°C?

3.1 Materials:

The Fe-C-Si alloy was prepared from 99.9% pure Fe,
99.99% pure C and 99.5% pure Si. Two alloys of approximate
composition Fe-C.75%C - 0.4%Si were made by melting appropriate
smount of iron, Carbon and milicon, Helting was done in an
induction furnace in argon atmosphere. The alloys were melted
twice to get a homogeneous button. Each time the alloys were
kept in the liquid state for about 15 minutes; for liquid state
homogenization. The alloy buttons were hot forged at about 1000°C
to 12.5 mm diameter red. These were than cold swaged to 10 mm
diameter red. These reds were vacuum scaled in a quarks tube.
The scaled rods were homogenized at about 1000°C for four days.
A piece was out from each of the rods and microstructure was
examined. No evidence of any seggregation was observed in one
of the rods. This rod was further reduced to 6 mm diameter by
cold exaging and cut in to small pieces of about 12 mm length.

The samples were chaminally analysed and the composition was found to be Pero,7490 + 0,37881.

3.2 Heat Treatment:

Austenitizing was done in a vertical resistance furnace 46 in nitrogen atmosphere. The nitrogen gas was passed through pyrogalal before entering the furnace. Pyrogalal solution absorbs oxygen from nitrogen. The samples were sustenitized for about 15 minutes at 850°C. The sample was then quenched in brine water. Since the M₂ temperature of steel with more than 0.6%C is below 0°C, the samples were given subzero treatment. This was done by requenching the samples in liquid nitrogen. Hardness of every quenched sample was measured and microstructure was seen to ensure that all of austenite has been transformed to martensite. The hardness of samples ranged from R₂ 62 to R₃ 65. It is necessary to start with a matensite matrix, because the nucleation of comentite is very fast and uniform distribution of comentite in ferrite matrix is obtained.

Temperings

The quenched samples were tempered in lead bath at 630°C, 660°C, 690°C and 710°C from time ranging from 5 hre. to 15 days. The temperature control was ± 5°C.

To avoid oxidation of the lead bath it was kept covered with charcoal powder all the time.

3.3 Metallography:

The tempered samples were ground, poliched and etched with 5% nitel and them unshed with water and alcohol to avoid formation of stains on the etched surface. The microstructure

3.2 Heat Treatment:

Austenitizing was done in a vertical resistance furnace 46 in nitrogen atmosphere. The nitrogen gas was passed through pyrogalal before entering the furnace. Pyrogalal solution absorbs oxygen from nitrogen. The samples were sustenitized for about 15 minutes at 850°C. The sample was then quenched in brine water. Since the M_f temperature of steel with more than 0.6%C is below 0°C, the samples were given subzero treatment. This was done by requenching the samples in liquid nitrogen. Hardness of every quenched sample was measured and microstructure was seen to ensure that all of austenite has been transformed to martensite. The hardness of samples ranged from R_g 62 to R_g 65. It is necessary to start with a matensite matrix, because the nucleation of cementite is very fast and uniform distribution of cementite in ferrite matrix is obtained.

Temperings

The quenched samples were tempered in lead bath at 630°C, 660°C, 690°C and 710°C from time ranging from 5 hre. to 15 days. The temperature control was ± 3°C.

To avoid exidation of the lead both it was kept covered with chargeal powder all the time.

3.3 Metallography:

The tempered complet were ground, polished and etched with 5% mital and them washed with water and alcohol to avoid formation of stains on the etched surface. The microstructure

was observed under a microscope whose eye piece and objective were kept same through out the investigation. Oil immersion objective was used to get better resolution. Total magnification was kept constant at X1000 to minimize relative errors.

Some of the photographs are given in the next chapter to illustrate the nature and shape etc.

3.4 Particle Size Measurement:

Direct measurement under microscope though possible was not accurate enough because at low times and temperatures the particle size was quite small and at X1000 magnification thickness of the cross wires will be comparable to many of the particle size. Equally difficult was to measure accurately the area of polished plane. Microfilm reader was tried. But though much more accurate, due to very high magnification (I19,6 coupled with X1000 of microscope), it was difficult to measure because all the particles were not exactly circular or elliptical and approximate ellipses had to be made out of particles. That meant to trace the particles on a paper first and then measure. This took as much effort and probably more time than making photographs, and then measuring the particle size, Also due to high magnification the comentite-ferrite grain boundaries got diffused which offset the accuracy obtained by high magnification. Hence photographs were made with 4 times enlargement to get a total magnification of 14000. The particle which were not exactly eigenlar of elliptical were approximated to the best possible ellipses. Major axis of each particle was measured. 350 to 450 particles were measured for each time-temperature

combination. The measurements were done by using a simple linear scale.

3.5 Magnification Calibration:

Actual magnification of photographs may not be necessarily same as obtained by numerical ratings of lenses. There are 5 factors which may cause error. (1) Errors in objective lense, (2) Errors in magnification of eye piece, (3) Error due to camera set up, (4) Film shrinkage after washing, (5) Improper length of microscope tube. To measure this error a standard stage micrometer was used with equally spaced fine lines on it. A photograph of the micrometer was taken with all the canditions as closely simulated to those in micrographs, as possible. The distance between 5 lines was measured at an apparent magnification of X4000. The ratio of this distance to the actual was the magnification. The magnification was found to be X2429. The correction factor due to the use of the apparent magnification m is given as

⁼ Apparent magnification = 4000 = 1.653.

CHAPTER 4

RESULES

4.1 Calculation of Particle Sise Distribution:

The major exis of the best fitting ellipse was measured for 350 to 450 particles for each tempering time. In order to obtain particle size distribution from these data, Dehoff's method 54 of quantitative metallography was used. This method was preferred because it is applicable to oblate spheroidal particles and it is simpler than other methods such as Sheil's method. Skepter's 54 method etc. Moreover most of the other methods are applicable to spherical particles only while in our photomicrographs the particle sections were both circular and elliptical which means that all particles were not spherical.

Dehoff's method 54

received to markly be a

If D__ be the meximum section size observed in a particular section size distribution and we make I section classes, the sise interval A is defined by the following expression.

The section with their major axis between 0 and A are kept in first size class. Sections with major exis between A and 2A are grouped in the second size class and so on. If I denotes the size class number and nes nos ne be the number of sections in tat, 2nd i-th and K-th size class respectively, them i-th size class will have particle

sections having major exes between $(i-1)\triangle$. and $i\triangle$. We want to convert this two dimensional size distribution. Let j denote the three dimensional size class and $H_1, H_2, \ldots, H_j, \ldots, H_k$ be the number of particles per unit volume in let, 2nd, ..., j-th and K-th size classes respectively. We want to find values of H_j 's from the values of H_j 's.

Dehoff assumed that (1) particles have the shape of an oblate ellipsoid of revolution and axial ratio of all the particles is same (2) distribution of particles in the matrix is random and showed that

$$\mathbf{w}_{3} = \frac{1}{A \triangle \mathbf{K}(\mathbf{q})} \sum_{i=1}^{\mathbf{K}} \mathbf{n}_{i} \beta_{ji} \qquad \cdots \cdots (55)$$

A . Area of plane of polish in which sections are measured

q . Axial ratio (ratio of minor to major axis)

K(q) Shape factor (a function of q)

For oblate spheroids

$$E(q) = \frac{q}{2} + \frac{2aq^{-1}\sqrt{(1-q^2)/q}}{2\sqrt{(1-q^2)}}$$
 ... (56)

3 = Seltykov's coefficient. These are available in tabulated form 53,59,60

Also the volume fraction of precipitate is given as:

Since we start with a martensitic matrix, distribution of commentite particles is expected to be random. Most of the

sections were either elliptical or circular but a few were difficult to be imagined as ellipses. Best fitting ellipses were curved out from these particles sections. There was no evidence of cigar shaped particles (plane section of prolate ellipsoids) and hence possibility of ellipsoids with prolate shape was ruled out.

Volume fraction of cementite can be calculated from the composition of the alloy, the densities of ferrite and cementite and the solubility of carbon in ferrite which is obtained from the literature ⁶¹. Densities of ferrite and cementite are also obtained from the literature ⁶².

The value thus obtained is the actual theoretical volume fraction of comentite. Volume fraction in the alloy used in this investigation was 0.117. Appropriate values of q are obtained by comparing calculated volume fractions from eqn. (56) and eqn. (57) with actual volume fraction.

From N, values the total number of particles may be obtained by the following equation.

$$\mathbf{H} = \sum_{i=1}^{K} \mathbf{H}_{i} \qquad \dots \qquad (58)$$

The mean particle size for each size class is

and the average particle size is

4.2 A Sample of Calculation:

Let us choose a set of calculations measured on the photomicrographs of a sample tempered for 1.011 x 10⁵ secs. at 690°C. Photomicrographs of this sample are given in Fig. 4(a) and the corresponding section sizes measured on these micrographs are given in table 2. It can be seen that the maximum size is 0.8 on on the micrographs.

For convenience section sizes were divided into eight section size classes. So K=8 and $\triangle=4.132\times 10^{-5}$. The corresponding section size distribution is given in table 3. Assuming different axial ratios (from 1.0 to 0.5) and using equation (56) and (57) the volume fraction V was calculated for each axial ratio. The values of K(q), V, \tilde{F} and H are given in table 4. It is clear that the exial ratio 0.98 gives best agreement with the actual value of 0.117. Once q is known H, is calculated using equation (55). All calculations were done on IRM 7044 computer. The computer programme is given in Appendix-I.

4.3 Resulter

The representative photographs of samples of tempered Pe = 0.74%C = 0.37%Si alloy are given in fig. 2 to 5 for all tempering times. The values of $\triangle_{\frac{1}{2}}$ K, \overline{F}_{2} , Y and N are listed in table 6 to 9. The variation of calculated volume fraction with the extal ratio is given in table 5. The calculated volume fractions are compared with the treatical value and the

selected values of q and V are listed in table 6 to 9. Using the selected values of q, values of F and N are calculated. These are also listed in table 6 to 9. The values of N, calculated after equation (55) are listed in table 10 to 13. The distribution of particles are presented in the form of histograms in fig. 6 to 9.

Table 2: The major exes of the best fitting ellipses corresponding to the particles in fig. 4 (tempering temperature 690°C and time 1.011 x 105 sec.). Area on the photomicrographs 297.63 cm. Total number of particles is 390.

Major axis measured on photomicrograph in mm.

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                                   4.0
                                        1.5
                                              1.5
                                                          4.0
                                                               4.0
2.0
      4.0
           5.5
4.0
                 3.5
                                              0.5
                       3.0
                             1.5
                                        4.0
                                                    4.0
                                                          3.5
3.5
      1.5
                                   5.0
                                                                2.0
                                                                3.5
      3.0
                                   1.0
      4.5
           3.5
                             4.5
                                        2,5
                                                    3.0
2.0
                 3.0
                       2.0
                                   1.0
                                              3.5
                                                          7.0
                                                               1.5
                       2.0
                                                          0.5
2.5
      2.5
           4.0
                 3.0
                                   0.5
                                              2.0
                                                    4.0
                                                                3.0
                                        3.5
            1.5
                       1.5
                             1.5
                                   1,0
                                              2.0
                                                    5.0
                                                          3.0
2.0
      3.0
                 4.0
                                                                3.5
```

Table 3: Section size distribution in the sample tempered at 690°C for 1.011x10⁵ secs.

Sise class interval \triangle = 4.132 x 10⁻⁵ cm.

Section	else	cless			Pends.	of	sections n _i	in	1-th g	roup,
	1			,			36			
	2	* * * * * * * * * * * * * * * * * * * *					95			
	3	·					95			
	4						83			
· · •	5						44			
	6		-				19			
	7		, , , , , , , , , , , , , , , , , , ,				13			
* **	8	* .		*			5			

Table 4: Variation of V, N, \overline{x} and K(q) on a exial ratio for tempering at 690°C for 1.011 x 10⁵ sees.

Axial ratio	Shape factor K(q)	Yolune fraction Y	redius F	of particles W per em ³ 10 ¹⁰
0.99	0.9966	0,1183	6,36	6,032
0.98	0.9933	0,1175	6.33	6.052
0.95	0.9835	0.1150	6,27	6.113
0,90	0.9673	0,1108	6, 16	6,215
0.85	0.9516	0, 1063	6,06	6,318
0.80	0.9362	0.1017	5.95	6,421
0.75	0.9213	0.0969	5,849	6.525
0.70	0.9068	0.0919	5,743	6,629
0.65	0.8929	0.0867	5,636	6.733
0.60	0.8795	0,0812	5.530	6,835

Table 5: Variation of volume fraction with axial ratio

Temperature •C	Time 10 ⁵	Axial ratio	Yolume fraction
630	1.749	0.7 0.65 0.58 0.55 0.5	0.136 0.128 0.117 0.112 0.103
	4.283	0.75 0.70 0.63 0.6 0.55	0.135 0.128 0.118 0.113 0.105
	9.15	0.65 0.6 0.55 0.5	0.134 0.125 0.117 0.107
	12.57	0.6 0.55 0.5	0.139 0.130 0.119
660	0.435	0.8 0.75 0.68 0.65	0.132 0.125 0.1167 0.112
	1.008	0.85 0.80 0.75 0.70 0.65	0.128 0.122 0.1167 0.110 0.104
	4.356	0.85 0.80 0.74 0.7	0.131 0.125 0.118 0.113
	8.46	0.8 0.75 0.70 0.65 0.6	0.131 0.125 0.118 0.111 0.104

The said offered the property of the said	Constituted by Long Strategic and Strategic	and interest of the Warry State of the Control of t	Anna de la companya del companya de la companya del companya de la
690	0.216	0.95 0.90 0.85 0.8	0.121 0.117 0.112 0.107
	0.417	0.9 0.85 0.78 0.70 0.65	0.130 0.125 0.117 0.108 0.102
* * * * * * *	1,011	0.98 0.95 0.9	0.117 0.115 0.110
	4.3332	0.6 0.55 0.52	0.131 0.122 0.117
710	0.204	0.75 0.70 0.65 0.60 0.55	0.131 0.124 0.117 0.109 0.102
	0.3984	0.95 0.90 0.85 0.80	0,121 0,1168 0,112 0,102
	0.984	0.85 0.80 0.78 0.7	0.124 0.120 0.117 0.108 0.102
	4.313	0.65 0.60 0.55 0.5	0.134 0.125 0.117 0.107

Table 6: Values of K, A, q, V, r and N at various tempering times corresponding to the tempering temperature of 630°C

Time (sec.) 10 ⁵	Sise class number K			Calculated Yolume fraction Y	Average radius F 10 ⁻⁵ cm	Total number of particles per unit volume, N 10
1.749	10	4.132	0,58	0.117	5,008	13.09
4,283	8	6,198	0.63	0.118	6.56	6.66
9.15	8	6.198	0.55	0.117	7.60	4.70
12.57	8	8.264	0.5	0.119	8,84	2.97

Table 7: Values of K, \triangle , q. V. \hat{r} and N at various tempering times corresponding to the tempering temperature of 660°C

Time (secs.) 10 ⁵	Sine olass number K	interval \triangle	Axial retio q	Calculated volume fraction V	Average rediue_5 F 10	Total number of particles per unit volume N 10 ¹⁰
0.435	7	4.132	0,68	0.1167	4,32	20,2
1.008	7	4. 132	0,75	0.1167	5,64	10,5
4.396	11	4. 132	0.74	0,118	7.73	3,177
8,46	10	6.198	0,7	0,118	9,36	2,26

Table 8: Values of K. A. q. V. T and N at various tempering times corresponding to the tempering temperature of 690°C

Time (secs.) 10 ⁵	Sise class number K	Sise class interval \(\triangle \) 10 ⁻⁵ cm	Arial Pasio Q	Calculated volume fraction V	redius F 10 ⁻⁵ em	Total number of particles per unit volume V 10 ¹⁰
0.216	7	4.132	0.9	0.117	4.01	21.27
0.417	7	4.132	0,78	0.117	4.79	11.14
1.011	8	4.132	0.98	0.117	6.33	6.05
4.3332	8	8.264	0.52	0.117	10.49	1.79

Table 9: Values of K, A, q, V, T and N at various tempering times corresponding to the tempering temperature of 710°0

Time (secc.) 10 ⁵	class	Sise class interval A 10 ⁻⁵ em	Arial retio q	Calculated volume fraction	rediue Fx10 ⁻⁵ em	Total mamber of particles per unit volume II 10 ¹⁰
0,204		4.132	0,65	0.117	5.16	12.45
0.3984	9	4. 132	0.9	0,1168	6,55	6,58
0.984	10	4.02	0,78	0,117	7.95	3.99
4.314	9	8,264	0.55	0.117	11.74	1,20

Table 10: Partiele size distribution for sample tempered at 630°C for various times.

8		1.749 × 10 ⁵ sees.		.285 x 10 ⁵ sees.	9.15	9.15 x 10 ⁵ sees.	12.57 × 10 ⁶	10 ⁶ secs.
		perticles in the 7th class		Particles in the jth class		Number of particles in the jth class	20 TO THE TOTAL TO	Number of particles in the jth class
2	1	6 00 00 E	\\	° # 00 00 00 00 00 00 00 00 00 00 00 00 0	\$ "} !	10 to ma-3	10 % ON 1	10 to am -3
•	8	8	3	0.5712	6.198	0.011	8.262	0,313
•		4.564	12.396	5.910	12,396	2,178	16,528	1,347
n		2,693	10.594	1.422	10,594	1.395	24.792	0.834
250	8,5	1,923	24-192	6.508	24.792	0,792	33,056	0,341
» (N	20,660	109*0	30.990	0,157	36.990	0.185	41.320	0.093
•	26.43	0,285	77. t88	0,082	77.188	0.093	49.584	0.017
-	28.8	901.0	43,386	0.020	43.386	0.033	57,848	0.013
•	33.036	0.057	19.584	0.01	19.584	0.019	66,108	0.011
0		883						
2		0,021						*
	A STATE OF THE PERSON NAMED IN COLUMN STATE OF THE PERSON NAMED IN				And the second second second second second			

Table its Particle aise distribution for the sample tempered at 660°C for various times.

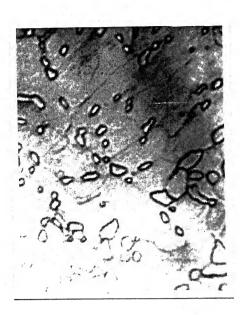
計.		Perfector (s		s, 1 particles in		AA	Ma.jor exte.	or Dumber of
			i i	6.00	Se Se		10-5 em	71, 10 to cm -3
		4.565	83	0,459	4.132	0,119	6,198	0.0652
64	1	8,700	188	2.50	8-264	**0	12,396	0.5683
*	8	663		7*787	12,396	1,055	16.594	0,7640
		88.3		1.596	16,528	1,028	24,792	0.5242
-		0,573	20,660	0,682	20,660	0.476	20.990	0,1691
10	24.73	48.5	24.792	0,251	24,792	0.307	37,188	0.0951
	136.63	0.101.0	28,924	=	28,924	0.199	43,386	0,0583
60					33,056	0.075	49,584	0,0038
0					37. 188	0.033	55.782	0,0123
2				* * * * * * * * * * * * * * * * * * *	41,320	0,025	61,980	0.0044
2					45.452	0,039		
	63	NPU						

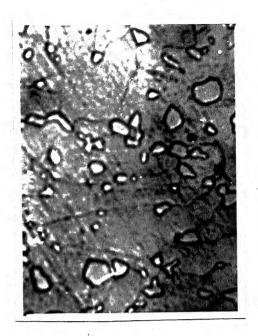
Table 12: Particle size distribution for the sample tempered at 690°C for various times.

		1000 QU × 93			5	1,011 x 10 sees.	4.332	4.5332 x 10 sece.
				perficient in the June		particles in the jth class		Number of the the the the the the olass
						7	8	
Made			3		Š		£ 70.	480
	3	Ž	8,264	Ş	8,264	1,718	16,528	0.573
		37.76	\$ 38	2.43	12,396	F	24.792	0*656
		***	8	1565	16,528	20.	33,056	0,269
	3	0.539	20,660	202	099*02	0.570	41,320	8.78
•			24.72	E a a	24.792	0,198	49.584	820.0
-	30.8	05000	10.8	6,155	88.924	9.76	97,948	88.0
-	7M-2	***			30°58	0,061	66,108	9,134

Table 15: Particle size distribution for the sample tempered at 710°C for various times.

8			966.79	**************************************	\$ 0.984	0,984 x 105 sees.	4.54	4.314 x 105 sees.
	H	Total Street		the 1th olass		Mumber of perficies in the jth class		Number of particles in the jth class
				6 8 3	(C)	10 to cm -3	\$ 0.2 8	10 to am-3
		97.8	4.132	555	4.132	\$ 5	8,264	1100
	8 260	***	4	1.741	8,264	0.539	16,528	0,4013
			12,394	2,050	12.394	1.000	24.792	0.5767
	16.525	6	16,525	1,515	16,525	1.058	33,056	0,1724
	50.8		150.08	675.50	20.03	0.878	41,320	0.1705
	8	681.0	24.788	0.272	24,786	0.321	49*284	0,0430
		0.219		88	28.924	0,186	57,648	0,0202
	2000		27.0%	6-00	33,056	0.054	26. 11.28	0,0159
				0,050	77.188	0,031	74.576	0,0026
						900		





Pig. 2(a). Fe-C-8i sample tempered at 630°C for 1.749x 10⁵ sees. Magnification: X2420

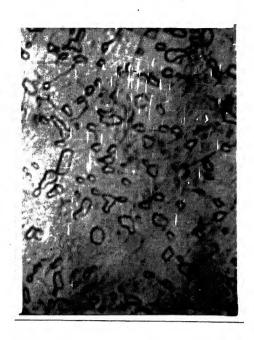
Pig. 2(b). Fe-C-Si sample tempered at 630°C for 4.283 x 10⁵ secs. Magnification: X2420





Pig, 2(c), Fo-C-81 sample temperad at 630°C for 9,15 x 10 secs, Magnification, 12420

Fig. 2(4). Fe-C-Si sample temper at 650°C for 12.57 x 10⁵ sees. Magnification: X2420



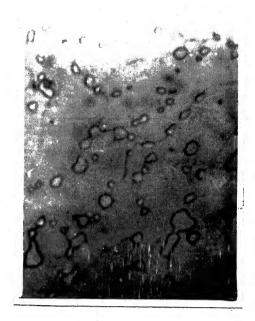


Fig. 3(a). Fe-C-Si sample tempered at 660°C for 0.435 x 10⁵ sees, Magnification: X2420

Pig. 3(b). Pe-C-Si semple tempered at 660°C for 1.008 x 105 sees. Magnification: 12420



10 seem Magnification: 12420 Magnification: 12420

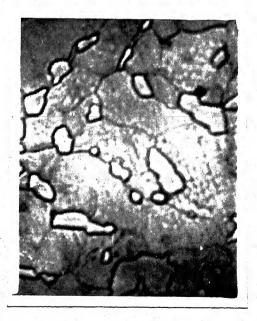
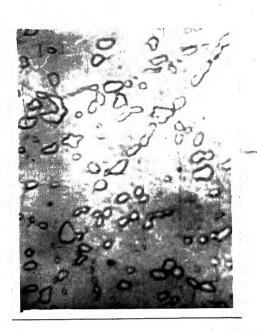


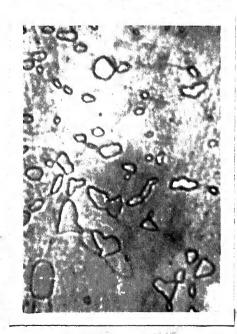
Fig. 3(d), Fe-C-Si sample tempered at 660°C for 8,46 x 10" mees.





10⁵ sees, Magnification: X2420 Magnification: X2420

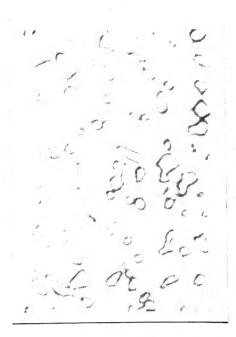
Pig. 4(a). Fe-C-Si sample Fig. 4(b). Fe-C-Si sample tempered tempered at 690°C for 0.216 x at 690°C for 0.417 x 105 secs.

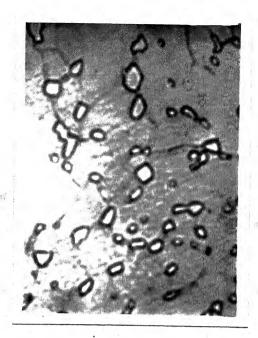


Pig. 4(c). Po-0-81 sample 690°C for 1.011 x



Fig. 4(d). Fe-C-Si semple tempered at 690°C for 4.3332 x 105 sees. Magnification: 12420 Magnification: 12420

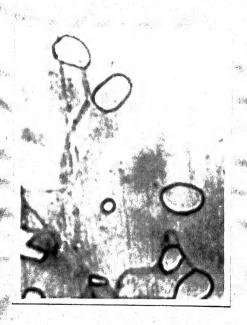




Pig. 5(a). Fe-C-Si sample tempered at 710°C for 0,204 x 10⁵ secs. Magnification: X2420

Pig. 5(b). Fe-C-Si sample tempered at 710°C for 0.3984 x 10⁵ secs. Magnification: X2420





Plg. 5(0). Po-C-Si emple Sumpared at 710°C for 0.984 x 10° esse. Magnification: X2420

Fig. 5(4), Fe-C-Si sample tempered at 710°C for 4.314 x 10⁵ sees. Magnification: X2420

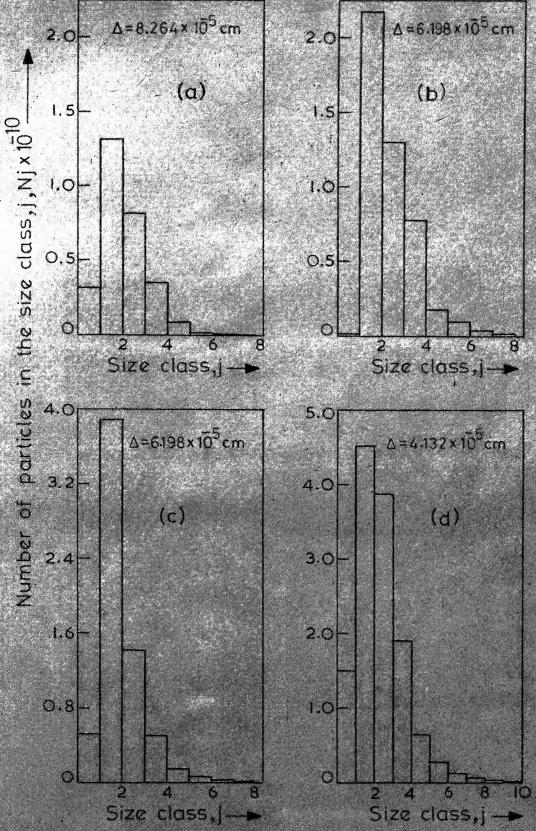


Fig. 6 Particle size distribution in the sample tempered at 630° C for (a) 12.57×10^{5} secs (b) 9.15×10^{5} secs (c) 4.283×10^{5} secs (d) 1.749×10^{5} secs.

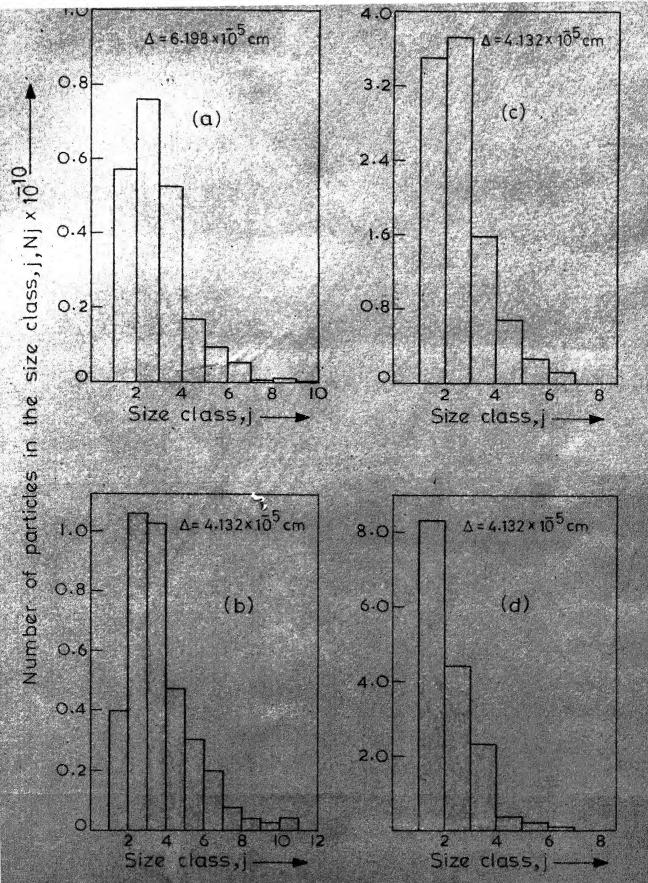


Fig. 7 Particle Size distribution in the sample tempered at 660°C for (a) 8.46 x 10⁵ secs (b) 4.356 x 10⁵ secs (c) 1.008 x 10⁵ secs (d) 0.435 x 10⁵ secs.

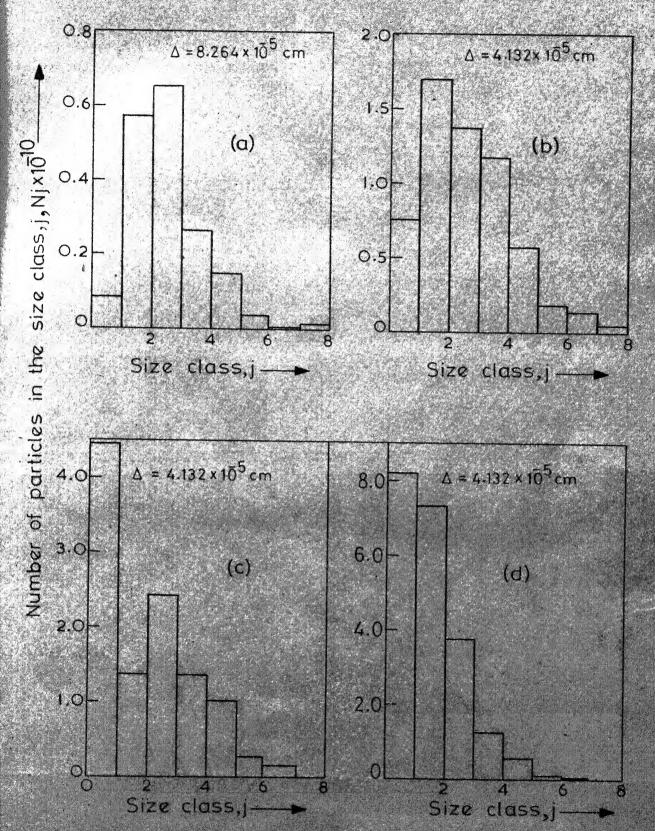


Fig. 8 Particle size distribution in the sample tempered at 690° C for (a) 4.3332×10^{5} secs (b) 1.011×10^{5} secs (c) 0.417×10^{5} secs (d) $0.216 \cdot 10^{5}$ secs.

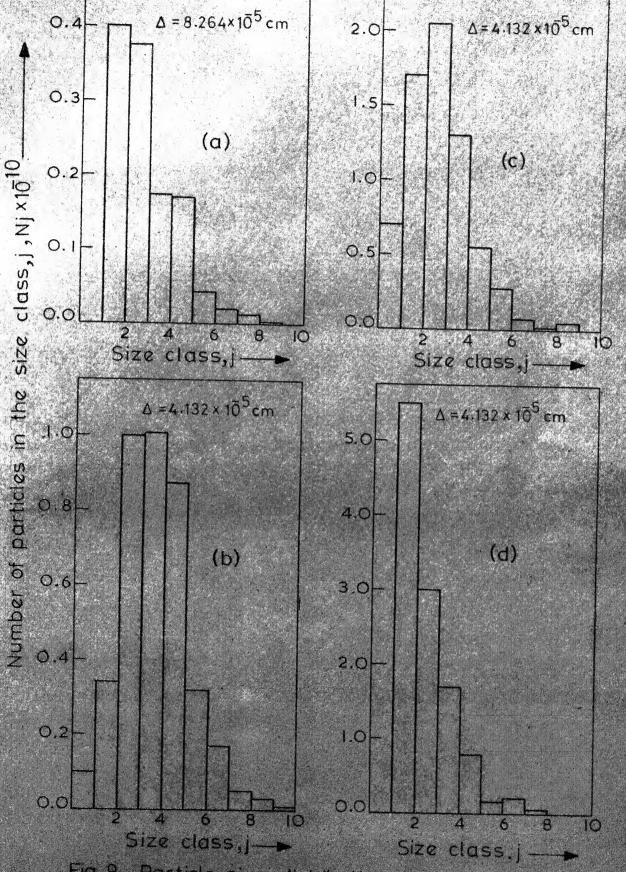


Fig.9 Particle size distribution in the sample tempered at 710° C for (a) 4.313×10^{5} secs (b) 0.948×10^{5} secs (c) 0.3984×10^{5} secs (d) 0.204×10^{5} secs.

CHAPTER 5

DISCUSSION

5.1 Error Analysis:

The scatter in the experimental value may occur due to the following sources of errors.

Limited resolution of optical microscope: This limitation puts a restriction on the size of particles which can be observed under microscope. This will give error in the evaluation of F, N, V etc. As is evident, the limited resolution will give over estimation of F and under estimation of N. Because of partial cancellation of these two epposing factors, the error in the volume fraction may not be significant. Quantitative estimation of this error is difficult. For large temperatures and times however, it may be safely assumed that error due to this factor is very small.

Magnification error: The actual magnification of the microscope set up may not be the same as that deduced from the specification of the lenses. Let,

M - Appearent magnification

It follows that,

Actual = (observed) X H (61)

A(cotual) - A(observed) × H2 (62)

where observed refers to value obtained using apparent magnifieation. It is clear that n_i values remain unaffected due to error in the magnification.

From equation (55), (58) and (60)

where

$$z = \sum_{j=1}^{K} \left[\sum_{i=j}^{K} n_{i} \beta_{j,i} \right] (1) \frac{(2+n)}{5} \sum_{j=1}^{K} \sum_{i=j}^{K} n_{i} \beta_{j,i}$$

Using equation (61) and (63)

From equation (55) and (56)

$$V = U \frac{\Delta^2}{\Delta^2} \qquad \qquad \dots \qquad (66)$$

where

$$U = \frac{\pi}{6 \times K(q)} \sum_{j=1}^{K} \left\{ \sum_{i=j}^{K} n_{i} \beta_{j+1}(i)^{3} \right\}$$

Using equations (61), (67) and (66) we get

Thus the error due to magnification does not change value of V.
Using a similar procedure it may be shown that,

Veing a stage micrometer, it was found that in this work
M = 1.653. Through out this investigation the lenses were kept

same and the same procedure was followed to obtain photograph of micrometer as was used to obtain micrographs.

Though the absolute values of F and N do change with error in magnification, the slopes of log F vs log t and log N vs log t remain uneffected. The experimental size distribution will be scaled down due to this error.

Error in measurement of section sizes:

As the particles were measured with ordinary scale it is but natural that error will be introduced in measurement. The minimum distance measurable was 0.05 cm. Therefore any distance below 0.025 can not be measured and hence this is the maximum error possible. Let us examine how \vec{r} , N and V change with this error. Let \pm e be the maximum error in measurement of section size. The maximum error in \vec{r} , N and V which can occur due to this factor can be calculated as follows.

Pirst add +e to all the section sizes measured for a particular sample and find out new section size distribution. From this, particle size distribution \tilde{r}_* , N and V can be calculated as described before. Let the new values be denoted by $(\tilde{r})_+$, $(V)_+$ and $(N)_+$. Now substract a from all the section sizes measured for the sample and calculate $(\tilde{r})_+$, $(V)_+$ and $(N)_+$ in a similar way.

Calculations were done for Fe-C-Si sample tempered at 690°C for 28 hre, with e = ± C₄O25 cm, on micrograph. It was found that meximum error found in F was 11.5% while that for Y and H was ± 12.4% and 14% respectively. The errors are not very

large when see that an error of \pm 20% has been reported in literature.

Error due to shrinkage of film:

For this the error analysis is exactly same as that for the error due to magnification due to micrographs. If,

5.2 Coarsening Kinetics:

A general equation for the variation of average particle with time can be written as

where n is a coefficient and K* is a constant. It has been shown that under certain conditions

n = 2 for interface controlled commening2

n = 3 for diffusion controlled commening2,5

n = 4 for grain boundary controlled coarsening 15,16

The constant K* is different for three cases. If $\vec{r}\gg\vec{r}_{o}$ we can approximate equation (69) by the following expression.

$$\log F = \frac{1}{n} \log K^* + \frac{1}{n} \log t$$
 . . . (70)

Thus from the slope of log F vs log t one can obtain information on the conrecting mechanism. The results of the present investigations were plotted as log F vs log t (Fig. 10) and the best fitting straight lines were drawn through the points. The

with time 51. The distribution function f(r,t) may be written

$$f(x,t) = P^2h_1(P) g(t)$$

where $P^2h_{\eta}(P)$ is a function of P only, $P = r/\overline{r}_{\eta}$ g(t) is a function of t only and $f(r_{\eta}t)$ is such that at a given time

$$\int_{0}^{\infty} f(\mathbf{r}, t) d\mathbf{r} = \mathbf{N},$$

Hence

$$H = \int_{0}^{\infty} f(\mathbf{r}, \mathbf{t}) d\mathbf{r} = \int_{0}^{\infty} \mathbf{P}^{2} \mathbf{h}_{1}(\mathbf{P}) g(\mathbf{t}) d\mathbf{r}$$
$$= g(\mathbf{t}) \mathbf{r} \int_{0}^{\infty} \mathbf{P}^{2} \mathbf{h}_{1}(\mathbf{P}) d\mathbf{P}$$

But according to the theory (see chapter II)

Hence

and

$$z(x,t) = \frac{1}{2} \times \frac{4}{9} \, x^2 h_1(x)$$
 * * * * (72)

Also

Combining equations (72) and (73)

$$P^{2}h_{1}(P) = \frac{9}{4} \frac{P}{(9+2)\Delta/6} \frac{H_{1}}{H}$$
 ... (74)

Under steady state condition the function $P^2h_1(P)$ should have a maximum at P=1.13 and should have a sharp cut off at P=1.5.

In order to compare the experimental size distribution with that predicted by the theory the function P²h₄(P) was evaluated using equation (74) and plotted against r₂/F for tempering temperatures 650°C, 660°C, 690°C and 710°C in figures 12, 15, 14 and 15 respectively. r₃ is calculated using equation (59),

The distribution curves show that the maxima do not occur at P = 1.15 although these are very close to P = 1.15 and tend to shift towards higher values of p with increase in time at a given tempering temperature. Also the curves do not show any sharp out off at P = 1.5. Each curve has a long tail. The tail becomes more prominent as the temperature is decreased. However at a given tempering temperature, the curves for different tempering times lie very close to each other. Thus the curves do not appear to have reached a steady state.

5.4 Determination of activation energy for the communication process

The constant K* in the general empirical equation (69) can be represented as the rate constant for the coarsening process. The empirical rate constants obtained from fig. 10 are listed in Table 14.

The activation energy for the process can not be determined

Table 14
Intercepts with statistical straight lines and straight line with slope 1/3 at various temperatures.

Temperature °C	Statistical intercept	Intercept with slope 1/3	Convening rate
630	-5.88	-6,07	6,166 x 10 ⁻¹⁹
660	-5.88	-5.95	1.413 x 10-18
690	-5.47	-5.85	2,818 x 10-18
710	-5.59	-5.75	5.623 x 10 ⁻¹⁸

from the values of empirical K* as the coefficient n appears to change with temperature. In order to obtain information about mechanism of this coarsening process, it is assumed on the basis of the results of the section 5.2 that the coarsening in the Fe-C-Si system is diffusion controlled. Hence after equation (15), $\tilde{\Gamma}^3 = K^*t$, the value of K* therefore can be obtained by plotting $\log r$ vs $\log t$ and then forcing the best straight line with a slope of 1/3. The intercept of this plot corresponds to 1/3 $\log K^*$. Such plots are shown in fig. 16 and the F* values are listed in table 14. A plot of $\log K^*$ vs $\frac{1}{2}$ in fig. 17 gives the average empirical activation energy of 51.03 heal/gm-atom. The constant K^* after equation (15) is given by

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The effective diffusion coefficient $D_{\rm eff}$ for the Pe-C-Si system after equation (23) is

Deff =
$$\frac{G_{p_0}}{G_C} \frac{V_p^2}{V_C^2} D_{p_0}$$

Hence

$$K^* = \frac{8 / V_{R}^2 O_0 O_{R0}}{9 RT O_0} \cdot \frac{V_{P0}^2}{V_{C}^2} \cdot D_{P0} \cdot \dots \cdot (75)$$

In this expression C_Q the average concentration of earbon in the matrix is close to C_p which is again close to C_e . Hence C_Q and these two terms may be cancelled from equation (75). The equation (75) becomes

$$K^* = \frac{3}{9} \frac{7}{R} \frac{C_{Po}}{V_0^2} \frac{V_{Po}^2}{V_0^2} \frac{D_{Po}}{V_0^2} \cdots (76)$$

Since the temperature dependence of the term in square bracket in eqn. (76) is negligible from 710°C to 630°C a plot of log K*T wa t/T should give a value for activation energy diffusion of iron in ferrite. Such a plot shown in fig. 17 yields a value of 53.305 Koal/gm-atom which may be compared with a published value of 60.0 Koal/mole for the self diffusion of Fe in -iron 66. Considering the assumptions involved the agreement is considered to be reasonable.

5.5 Growth of individual particle

Debut 65 has recently suggested a method for obtaining the growth rate of individual particles from a size distribution of these particles in the system. If N(r,t) be the number of particles per unit volume of size r, at time we can define a quantity $N(\cdot)$ r,t) which gives the number of particles of size

greater than r at time t in the following manner.

$$N(>r,t) = \int_{r}^{r} N(r,t) dr \qquad (77)$$

where r is the size of the particle and r_{max} is the maximum size at time t. If it is assumed that the growth path of individual particles do not cross the value of function N(> r,t) will be some for a given particle at all times. This suggests a method for graphically obtaining the growth rate of any particle.

In the iron-carbon-cilicon system considered here the growth path of individual particles during coarsening are unlikely to cross each other. Hence above procedure may be applied. In terms of particle size distribution N_j, the equation (77) may be written the following manner.

where K represents the size class containing particles of maximum size r and $r_s = \frac{(2+\alpha)}{5}$ ($j\triangle$). Pige, 19 to 26 show the plots of $H(>r_s)$ i.e. $\sum H_s$ against r_s for the Pe = 0.7460 = 0.37631 alloy tempered at 630°C, 660°C, 690°C and 710°C for various times. Cross outs were taken from these curves at constant $H(>r_s)$ in several positions. These cross outs are indicated in the figs, 19 to 26. They give the values of r of a given particle at different times at a given temperature. The change in the value of r with time obtained in the cross outs are shown in the fig. 27 to 34. It is to be noted that figs.

ty, 21, 23, 25, 26, 29, 31 and 32 show the decrease in size of small particles where as figs. 20, 22, 24, 26, 27, 30, 33 and 34 show that larger particles increase with time and the growth rate is large when time is small and decreases with increase in time. The growth rate of particles at the tempering times of 4.283 x 10⁵ secs., 1.011 x 10⁵ secs. and 0.984 x 10⁵ secs. at temperature of 630.0, 660.0, 690.0 and 710.0 respectively are obtained from gfigs. 27, 28, 29, 30, 31, 32, 33, and 34. The growth rates thus obtained are plotted against x for the above mentioned time and temperature. These are shown in fig. 35, 36, 37 and 38. These figures show that the growth rate is negative at smaller sizes, becomes positive at larger sizes and tends to approach a maximum. The maximum in growth rate occurs approximately at x = 27 at 630.0 and 710.0 (Fig. 35 and 38) and the growth rate is sere at about x = 7.

The above result is consistent with Greenwood's theory. This theory suggests that $x \stackrel{dv}{dx} ve \stackrel{1}{x}$ is linear. Such plots are shown in figs. 39, 40, 41 and 42. The slope of these lines at 630°C, 660°C, 690°C and 710°C are 5.6 x 10⁻¹⁷ om /sec., 15.9 x 10⁻¹⁷ om /sec., 1.06 x 10⁻¹⁷ am /sec. and 0.5 x 10⁻¹⁷ om /sec. respectively. These values may be compared with values of 6.75 x 10⁻¹⁷, 10.49 x 10⁻¹⁷, 10.25 x 10⁻¹⁷ and 23 x 10⁻¹⁷ om /sec. calculated from equation (9) using values of /= 700 ergs/cm². The diffusion coefficient of earlies D = 0.02 exp (- $\frac{20100}{100}$). The values of F calculated from these plots are (- $\frac{2700}{100}$). The values of F calculated from these plots are 9.7 x 10⁻⁵ om, 10.5 x 10⁻⁵ om, 9.5 x 10⁻⁵ on and 6.6 x 10⁻⁵ om.

710°C, 690°C, 660°C and 630°C respectively. These values may be compared with the experimental values of 7.93 x 10⁻⁵ cm, 6.33 x 10⁻⁵ cm, 7.73 x 10⁻⁵ cm and 6.56 x 10⁻⁵ cm at 710°C, 690°C, 660°C and 630°C respectively. The agreement is considered good because the accuracy is not expected to be high. It was possible to have only limited number of points on the graph. Thus inspite of its simplicity, Greenwood's theory of diffusion controlled coarsening seems to be in reasonable agreement with our experimental results. This analysis also supports our earlier conclusion that the coarsening process in Pe = 0.74%C = 0.37%Si alloy at 630°C, 660°C, 690°C and 710°C is diffusion controlled.

5.6 Determination of surface energy

Surface energy Y can be evaluated from equation (75) by substituting the values of all other terms. However, Ardell 15 has pointed out that equation (75) for ${}^{*}K^{5}$ is strictly valid when the volume fraction of comentite is nearly zero. The volume fraction of comentite in the Pe-C-Si alloy used in this investigation &c 0.117. The equation (75) may be written after Ardell 13 as

where $\mathcal V$ is a function of volume fraction of computite. The value of $\mathcal V$ calculated from Andell's expression for the volume fraction 0.117 of commutate to 0.06. The value of $T_{\rm q}$, the difference in the volume of one sole of $T_{\rm q}$, and $\mathcal V$ make of $\mathcal V$ in fearity is

2.1 cm³/mole.⁶⁷ The other values are given below: Concentration of iron in ferrite, $C_{pe} = 0.14 \text{ mole/cm}^3$ Values of comentite per mole of carbon, $V_m = 24.3 \text{ cm}^3/\text{mole}$.⁶⁷ Melar volume of iron in ferrite, $V_{pe} = 7.09 \text{ cm}^3/\text{mole}$.⁶⁷ Diffusivity of iron in ferrite, $D_{pe} = 2.0 \text{ exp} \left(-\frac{60000}{RT}\right)$.

Substituting these values in equation (78) surface energies of 874, 800, 1130, and 1110 ergs/cm² are found at 710°C, 690°C, 660°C and 630°C respectively. Thus it is seen that these results are in very good agreement with expected value of about 700 ergs/cm².

5.7 Effect of milicon on coarsening kinetics

Fortunately the results of an investigation carried out in this laboratory on the coarsening kinetics of generatite in an Fe - 0.79%C alloy at 650, 660, 688 and 712°C are available. These results show that in this temperature range the coarsening is diffusioncontrolled but the particle size distribution does not approach a steady state. A similar behaviour was observed in this investigation in the Fe-C-Si alloy. e empirical activation energy of coarsening of 52.17 Keal found in the iron carbon alloy is close to the value of 51.03 Keal found in the Fe-C-Si alloy. However, the values of coarsening rate constant E found in the Fe-C-Si alloy are only about 40% of the values of Ke found in the Fe-C alloy. Thus the presence of silicon considerably reduces the rate of coarsening. The surface energy of cementite found in the Fe-CoSi alloy 874, 800, 1130 and 1110 ergs/on are also much less than the values of 2290, 1850, 2020

and 2700 ergs/cm² in the Pe-C alloy. It is thus clear that the presence of silicon considerably reduces the interfacial energies between comentite and ferrite which in turn is responsible for slower coarsening rate of comentite particles.

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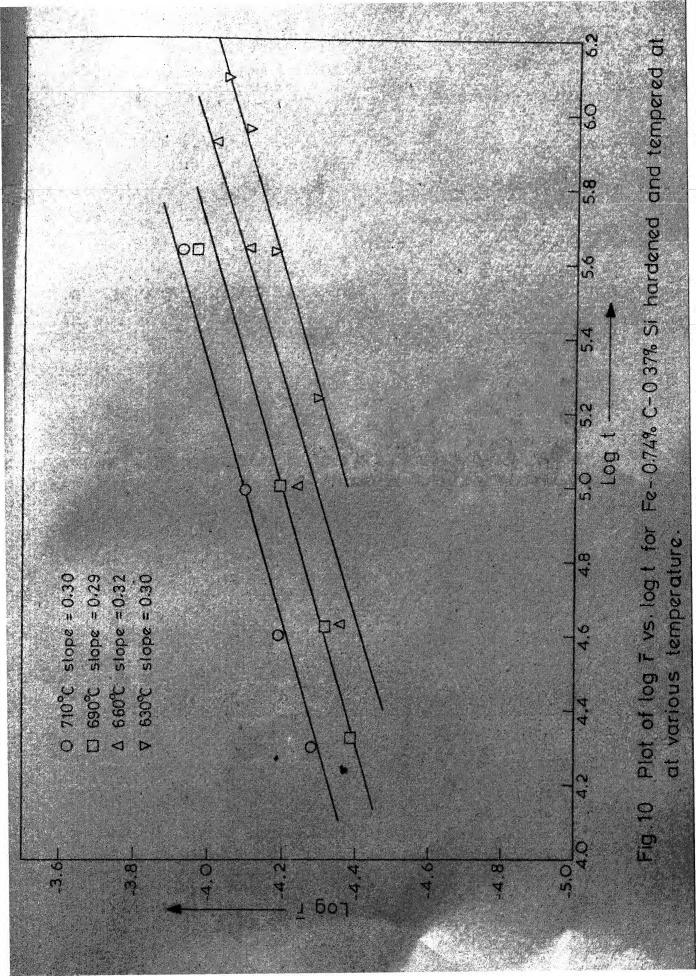
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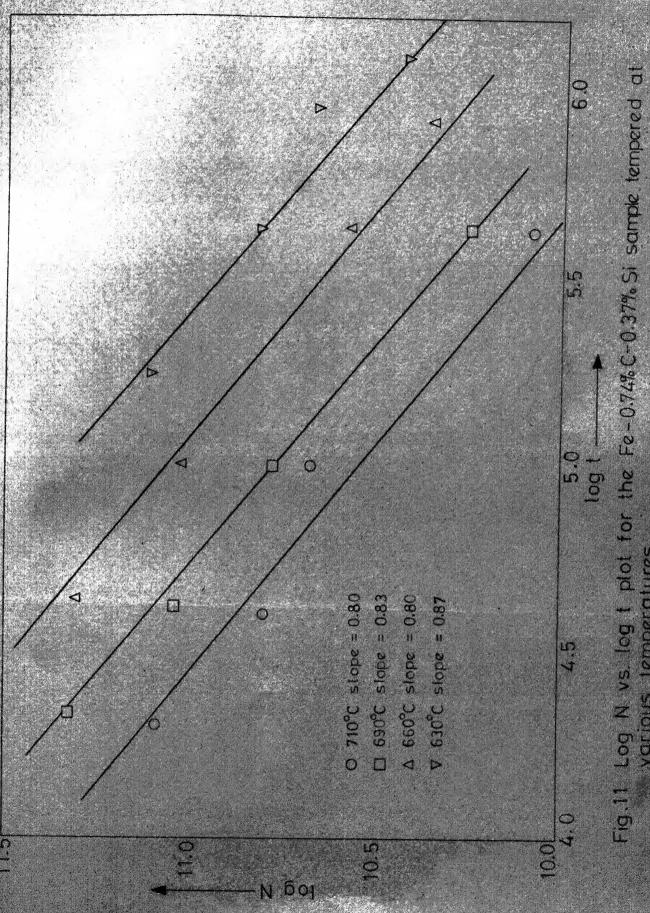
CHAPTER 6

SUMMARY AND CONCLUSIONS

Samples of steel containing 0.74%C and 0.37%Si were hardened and tempered at 710°C for 5 hrs, 11 hrs, 27 hrs and 120 hrs, at 690°C for 6 hrs, 12 hrs, 28 hrs and 120 hrs, at 660°C for 12 hrs, 28 hrs, 120 hrs and 240 hrs and at 630°C for 48 hrs, 120 hrs, 240 hrs and 350 hrs. The particle size distribution in these samples was determined and the results were analysed in terms of theories of coarsening. The following conclusions were drawns

- (1) log F vs log t plots were straight lines with slopes of about 0.29 to 0.32
- (ii) log N ve log t plote were straight lines with a slope of 0.80 to 0.87
- (iii) Although the above results suggest that the coarsening is diffusion controlled, the particle size distribution did not reach a steady state.
- (iv) Activation energy calculated from coarsening rate constant is 53.3 Kcal/gm-atom, which is close to that of diffusion of iron in —iron.
- (v) The coarsening rate constants K* in the presence of the silicon are about 40% of those in the pure iron carbon.
- (vi) Interfacial energy of comentite-ferrite interface was found to be around 950 ergs/cm². Thus silicon appears to decrease the interfacial energy.
- (vii) Thegrowth rate of individual particles was determined by applying a new method. The results obtained also indicate coarsening to be diffusion controlled.





various temperatures

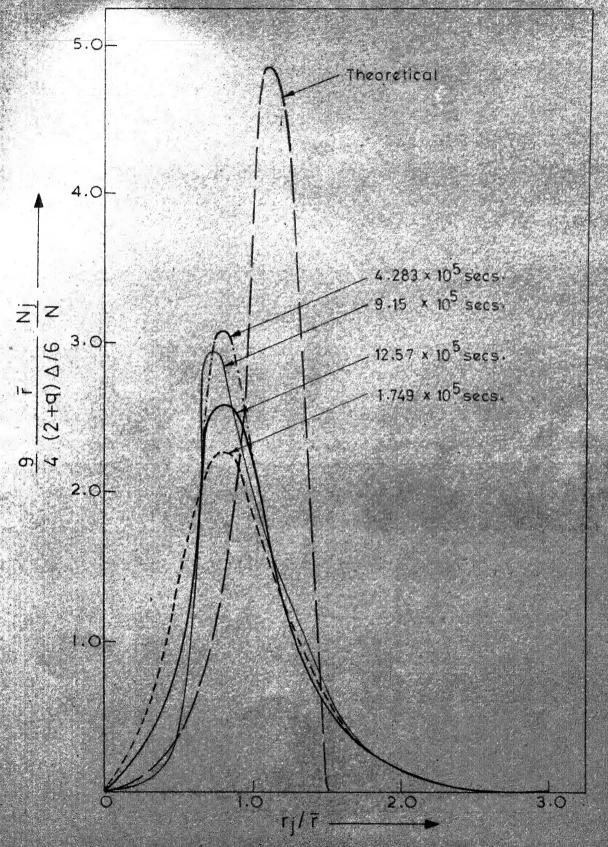


Fig.12 The normalised size distribution curve for the sample tempered at 630°C.

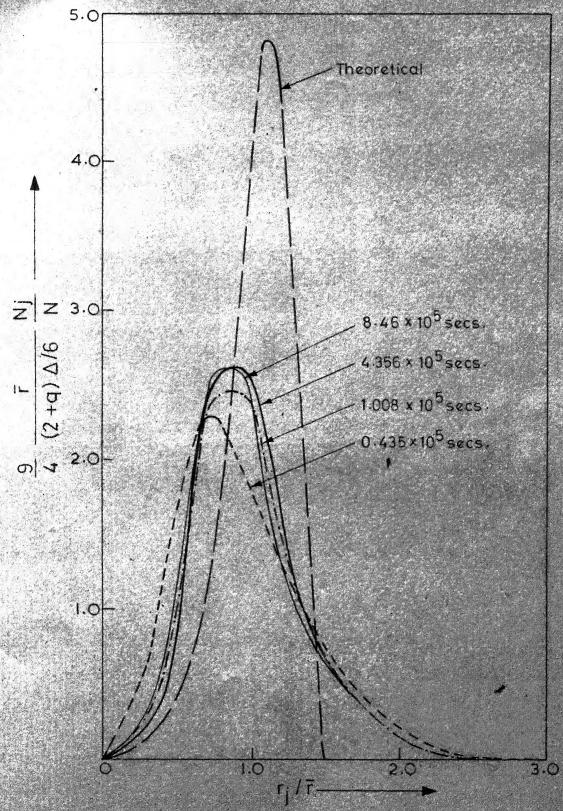


Fig.13 The normalised size distribution curve for the sample lempered at 660°C.

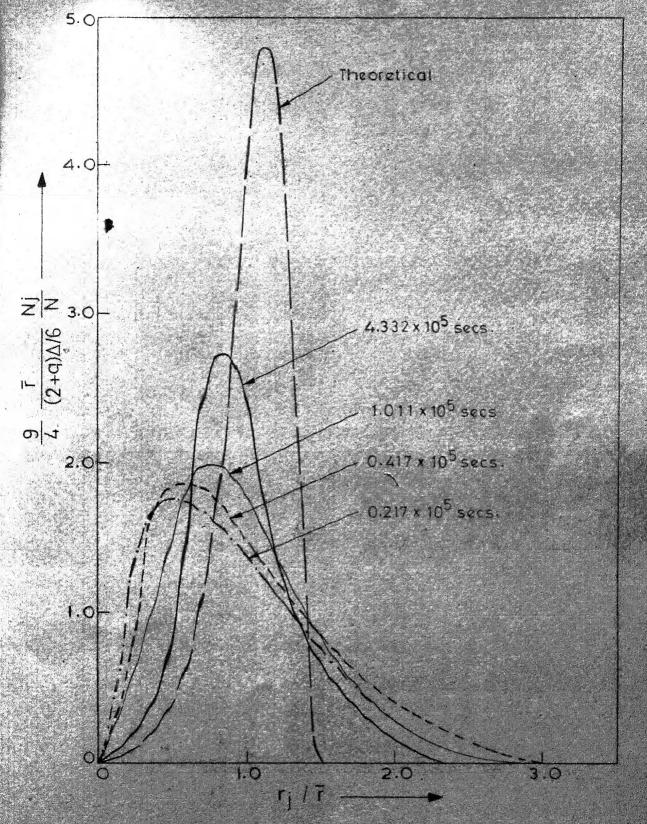


Fig.14 The normalised size distribution curve for the sample tempered at 690°C.

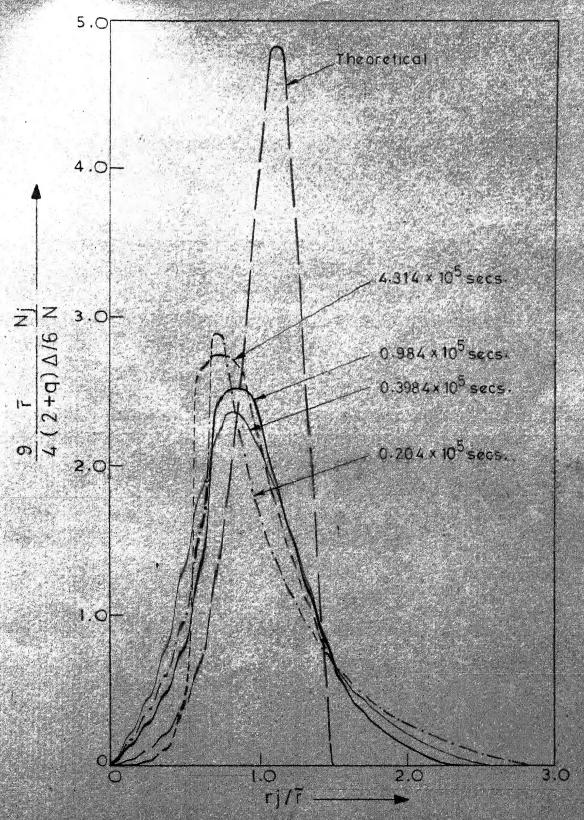
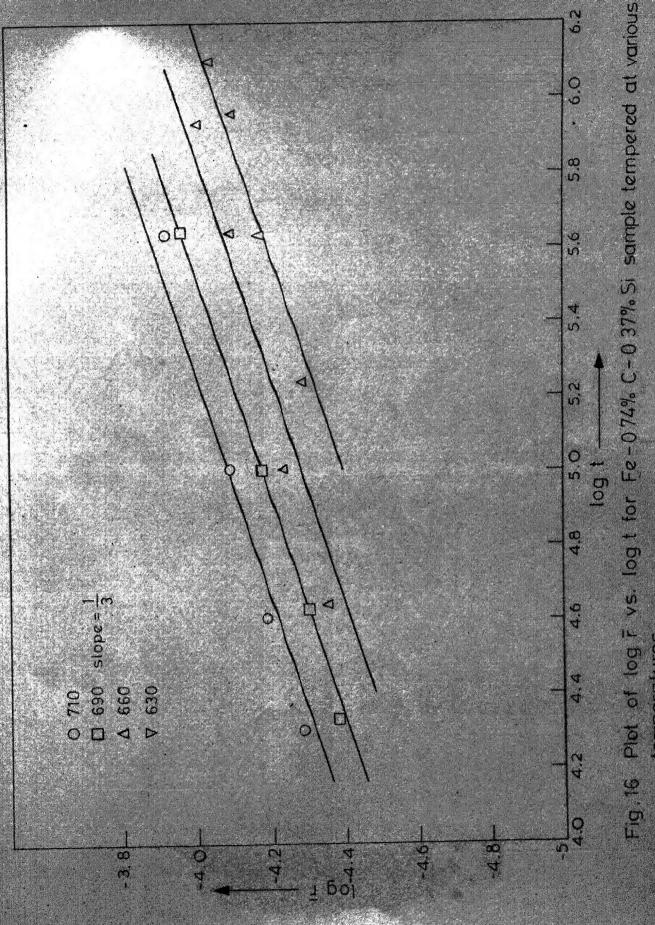


Fig. 15 The normalised size distribution curve for the sample tempered at 710°C



temperatures.

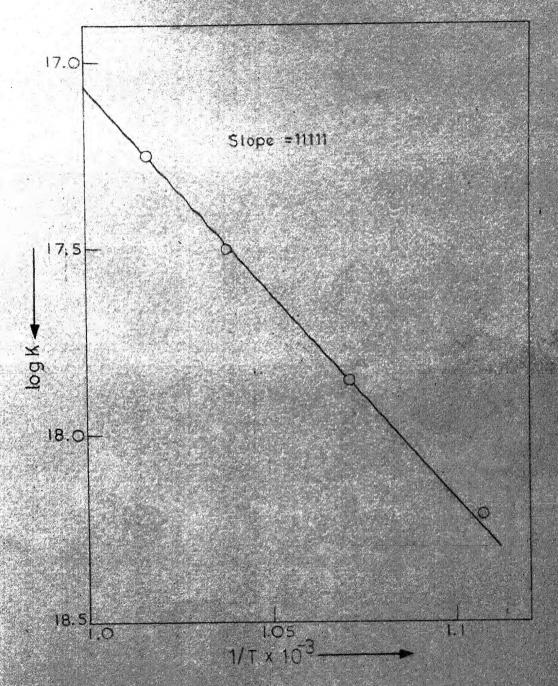


Fig. 17 Plot of log K vs. 1/T

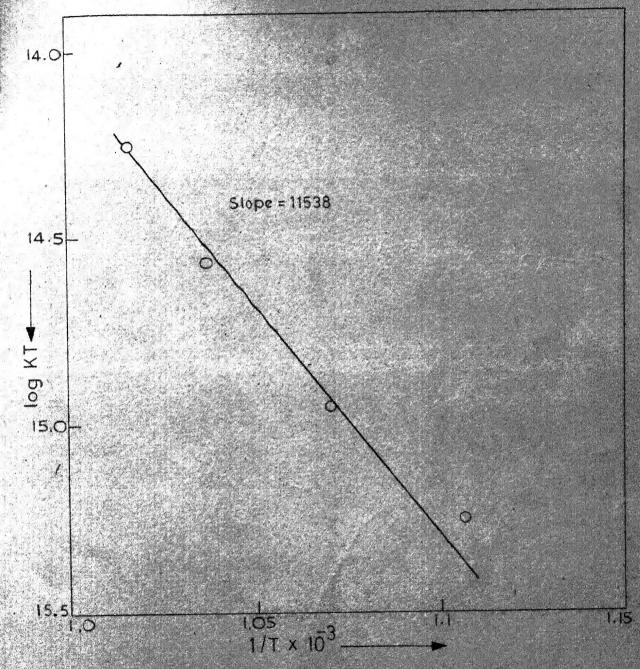


Fig. 18 Plot of log KT vs. 1/T

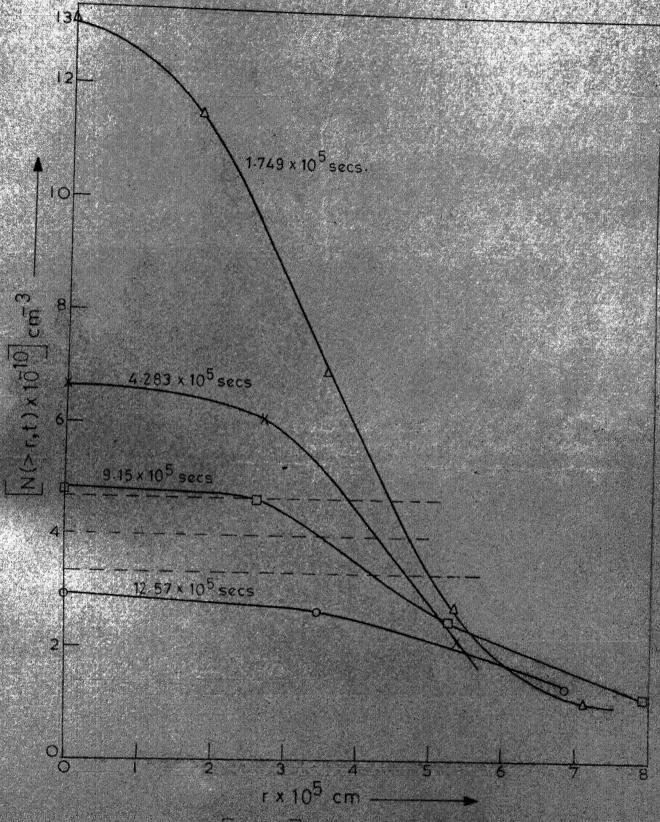
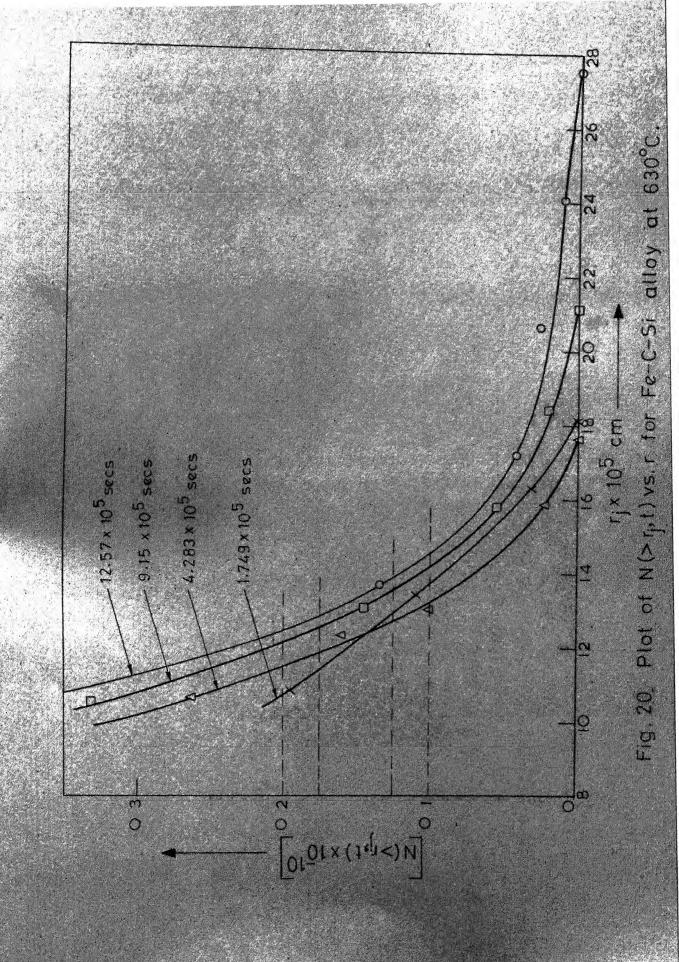


Fig. 19 Plot of [N(>r,t)] vs.r for Fe-C-SI sample tempered at 630°C.



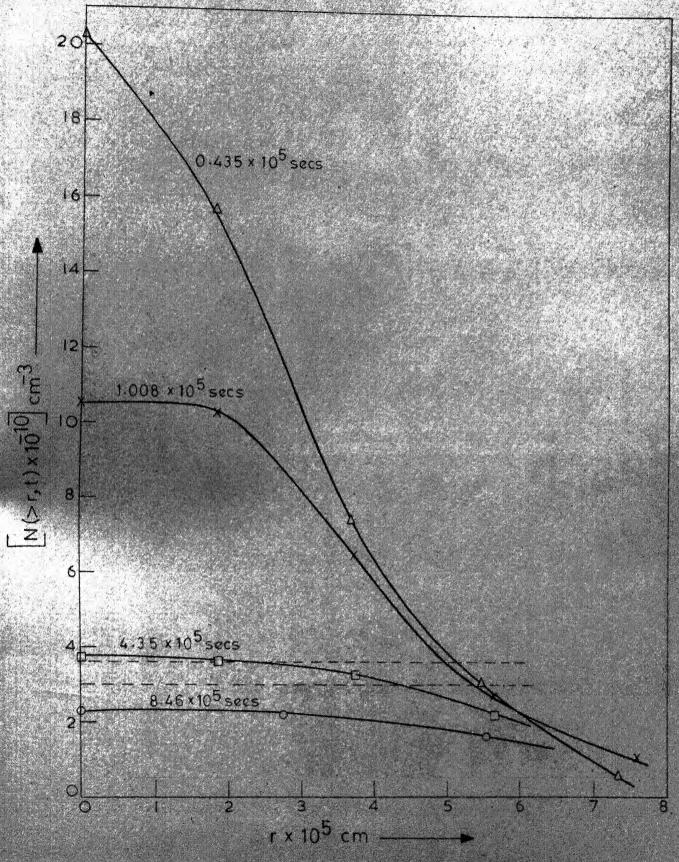
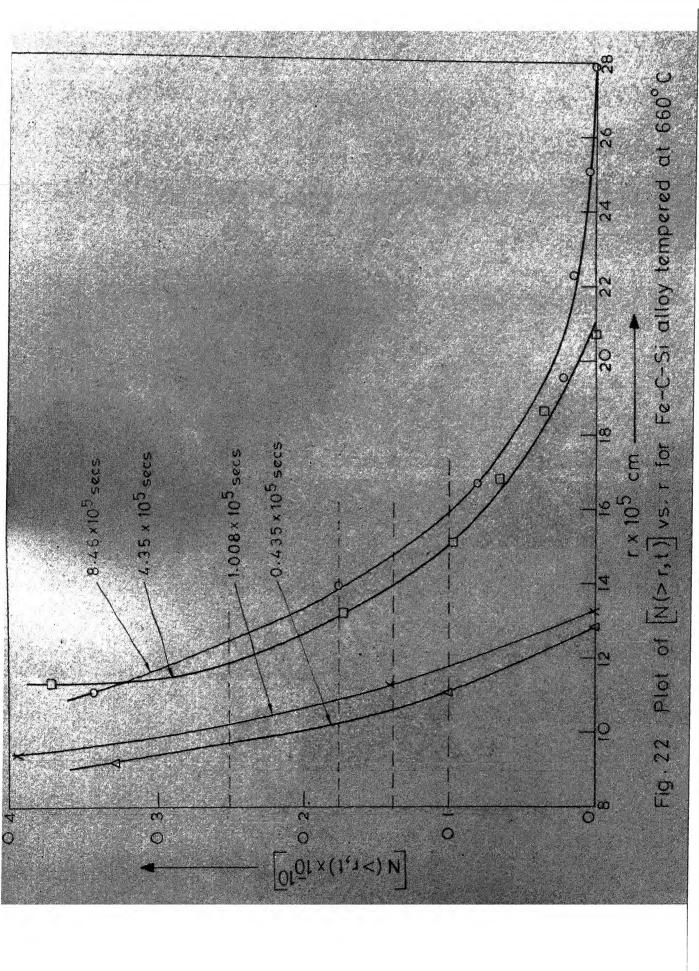


Fig. 21 Plot of N(>r,t) vs.r for Fe-C-Si alloy tempered at 660°C.



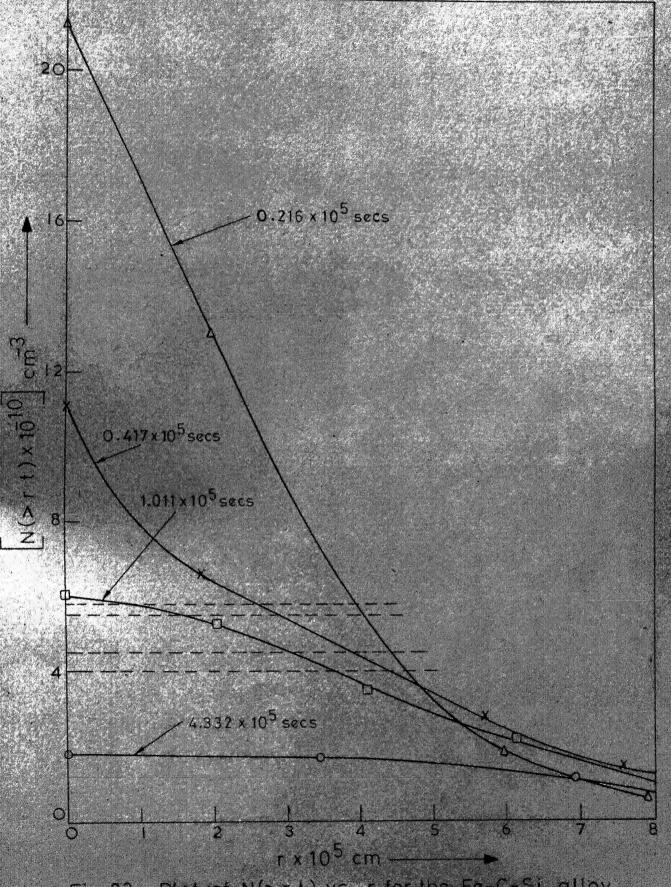
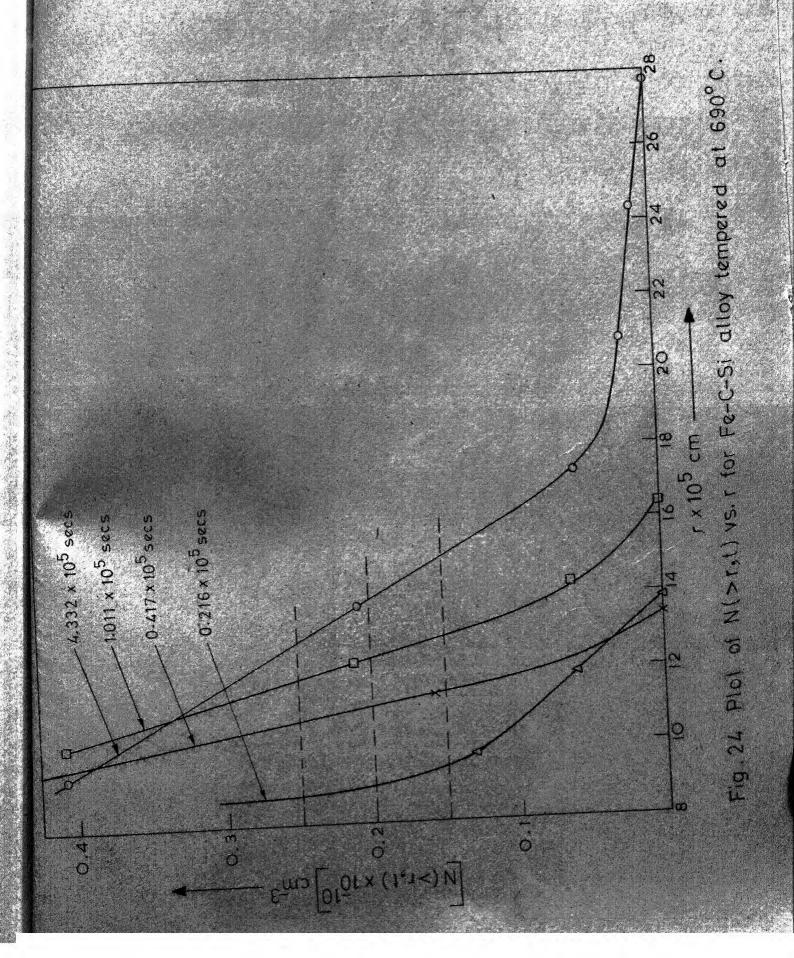


Fig.23 Plot of N(>r,l) vs. r for the Fe-C-Si alloy tempered at 690° C.



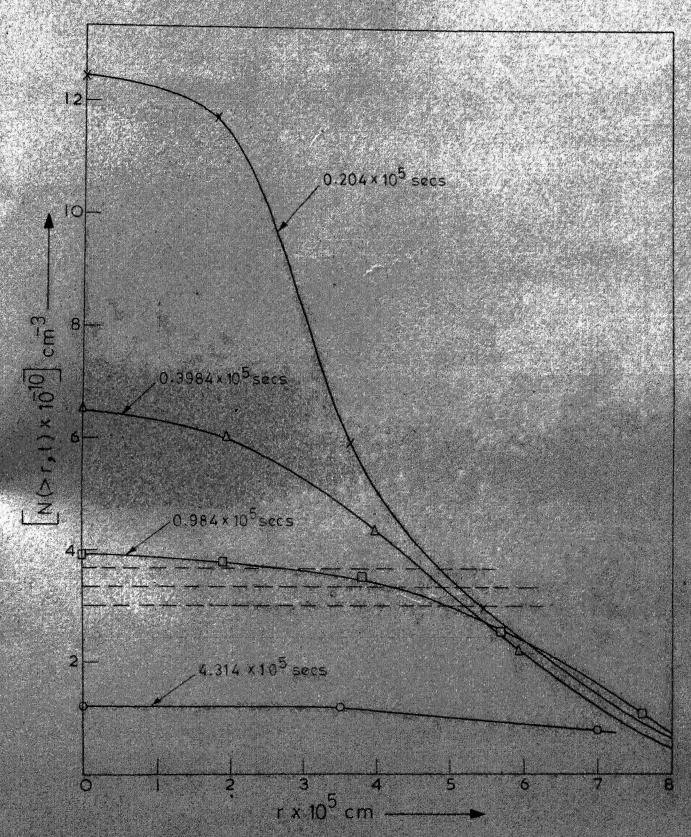
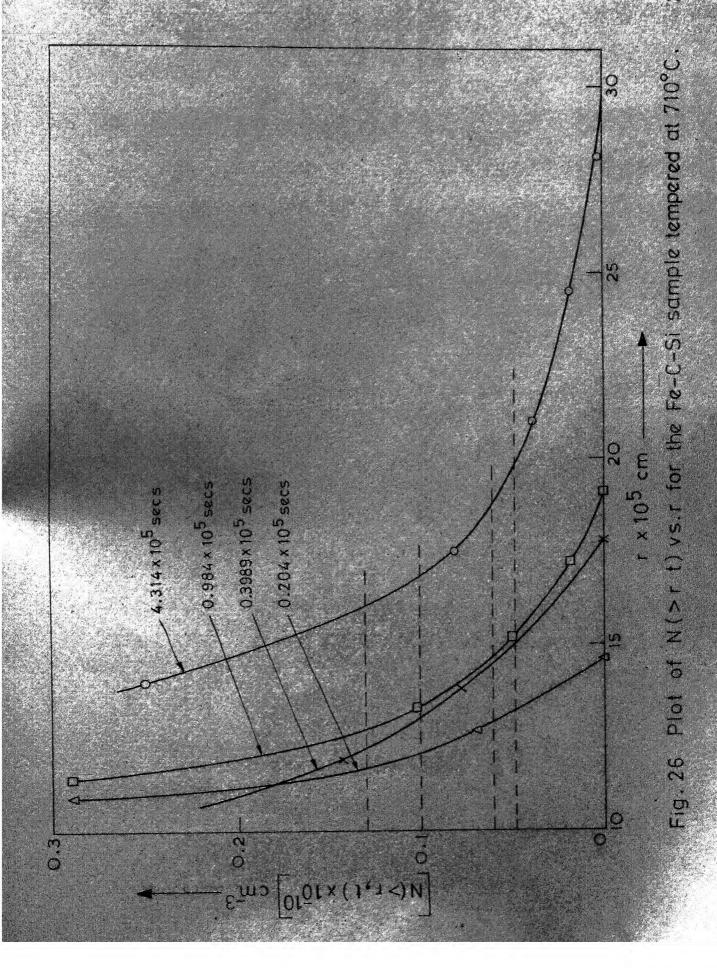


Fig. 25 Plot of N(>r,t) vs r for Fe-C-Si alloy tempered at 710°C.



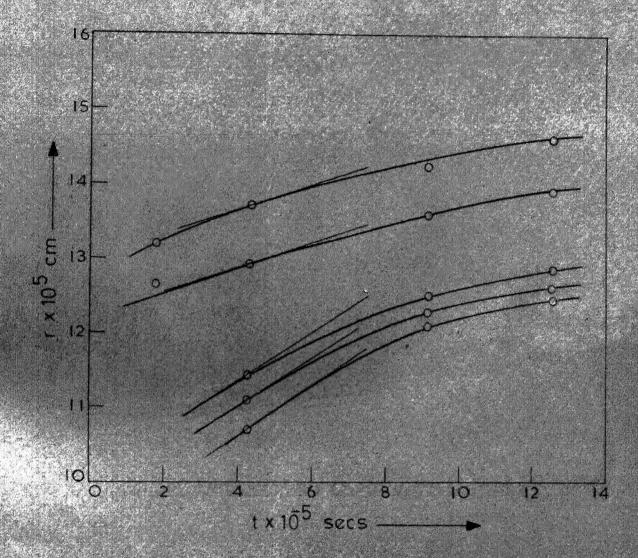
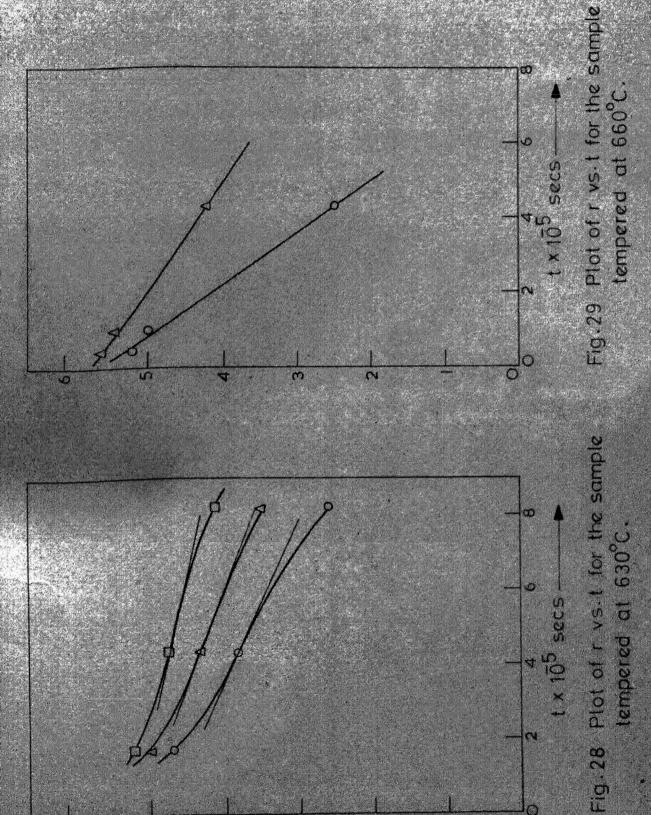


Fig. 27 Plot of r vs. t for the sample tempered at 630° C.



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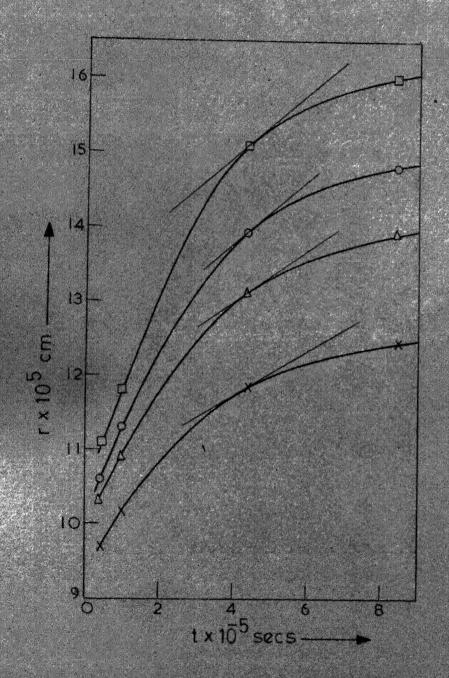
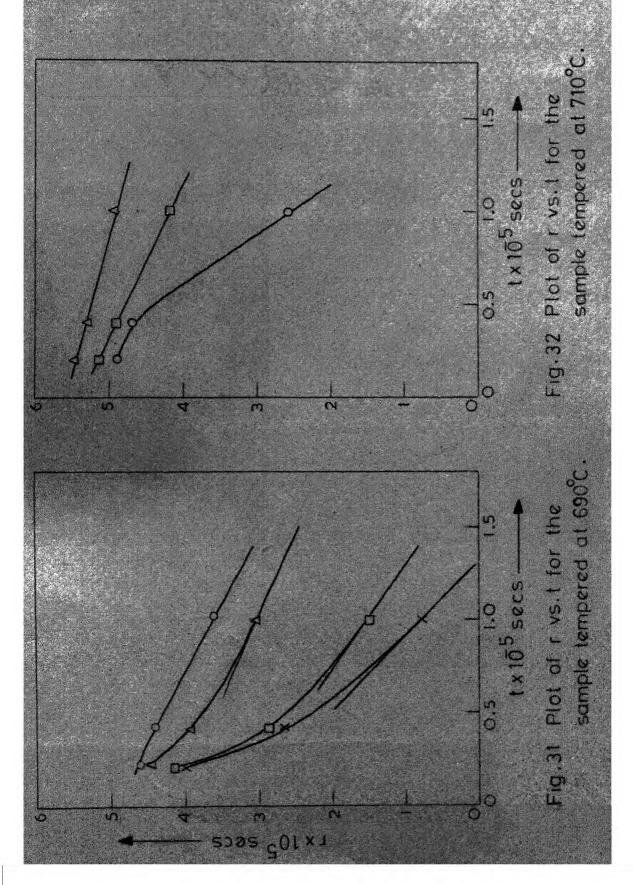


Fig. 30 Plot of r vs. t for the sample tempered at 660°C.



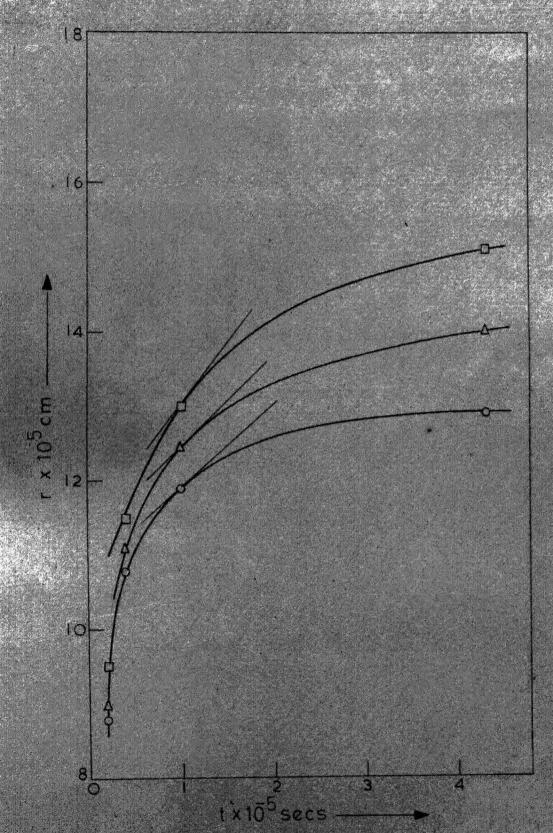


Fig. 33 Plot of r vs. t for the sample tempered at 690°C .

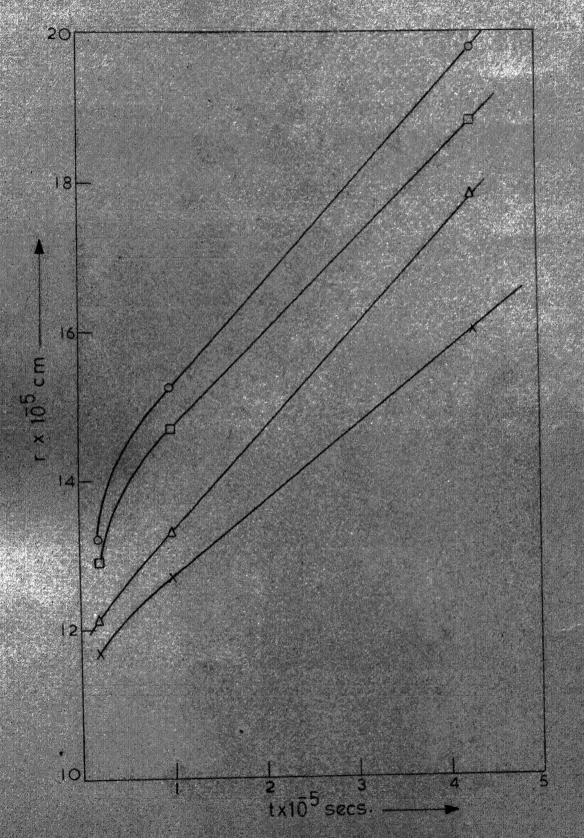


Fig. 34 Plot of r vs. t for the sample tempered at 710° C.

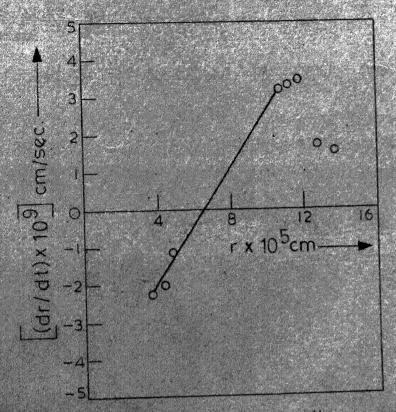


Fig.35 Plot of dr/dt vs.r for the sample tempered at 630°C.

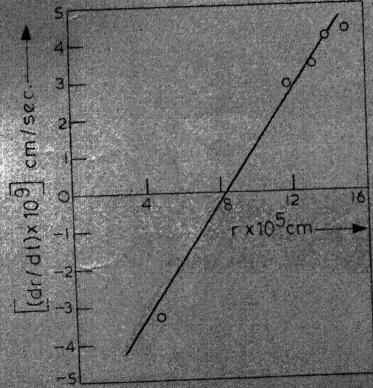


Fig. 36 Plot of dr/dt vs.r for the sample tempered at 660°C.

Fig.38 Plot of dr/dt.vs.r for the sample tempered at 710°C.

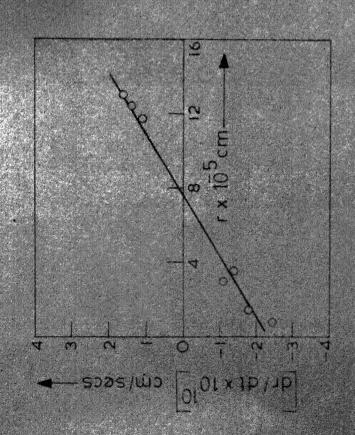
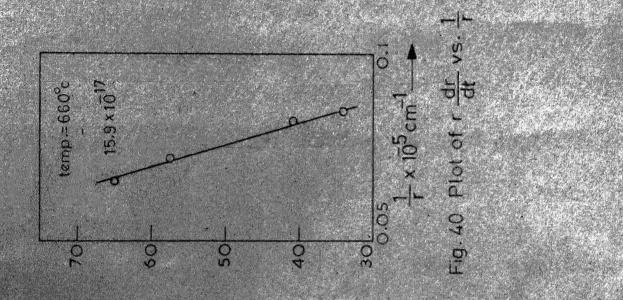
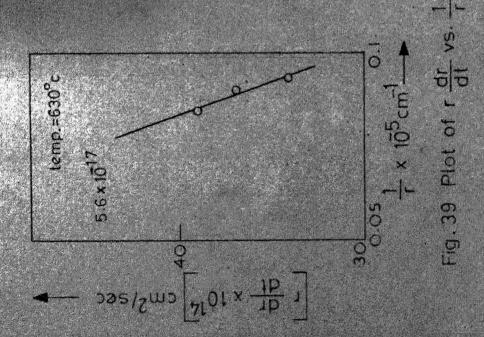
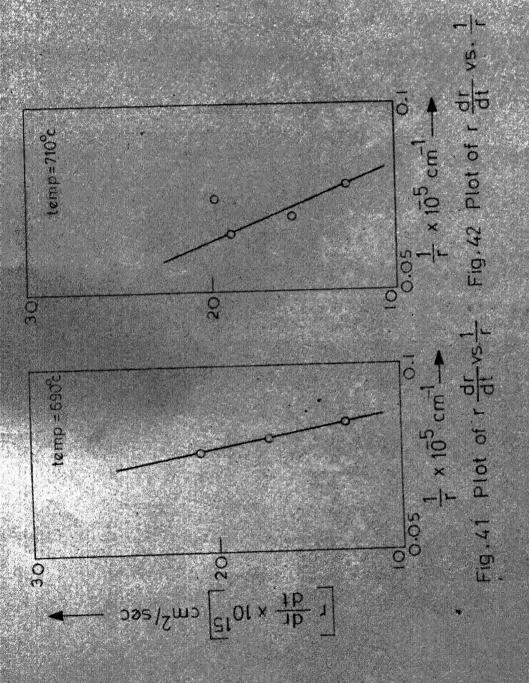


Fig. 37 Plot of dr/dt vs.r for the sample tempered at \$90°C







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